

# Guided Model Checking for Programs with Polymorphism

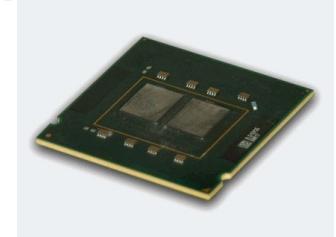
Neha Rungta & Eric Mercer

Computer Science Department, Brigham Young University, Provo, UT, USA

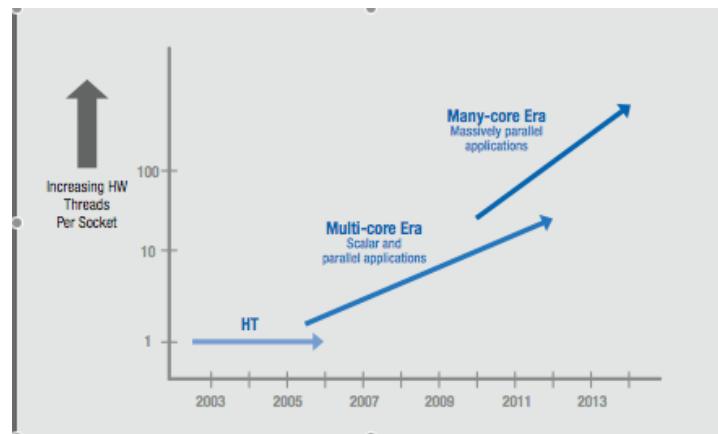
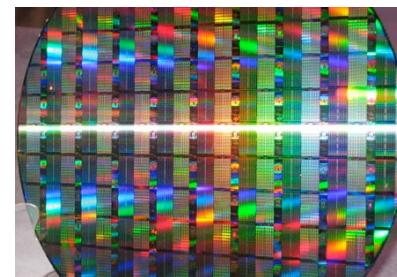
# Current Trend



Dual and Quad Core Processors are becoming increasingly common



Intel's 80 core prototype



More processors on a single die \*

\* Image courtesy Intel white paper

# Multi-threaded Programs

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- ▶ Threads contend for shared resources
- ▶ Locks used to force exclusive access
- ▶ Incorrect usage leads to errors
- ▶ Deadlocks and race conditions are problematic
- ▶ Scheduling determines execution order
- ▶ Certain execution order cause errors

# Software Model Checking

---

$P_a$

```
a0: while True do  
a1:   wait (turn = 0)  
a2:   turn = 1  
        end while
```

$P_b$ :

```
b0: while True do  
b1:   wait (turn = 1)  
b2:   turn = 0  
        end while
```

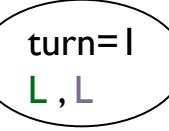
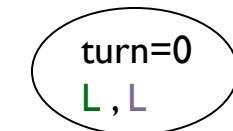
# Software Model Checking

$P_a$

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a0: while True do  
a1:   wait (turn = 0)  
a2:   turn = 1  
        end while
```

$P_b$ :

```
b0: while True do  
b1:   wait (turn = 1)  
b2:   turn = 0  
        end while
```



# Software Model Checking

```
Pa
a0: while True do
    a1: wait (turn = 0)
    a2: turn = 1
    end while

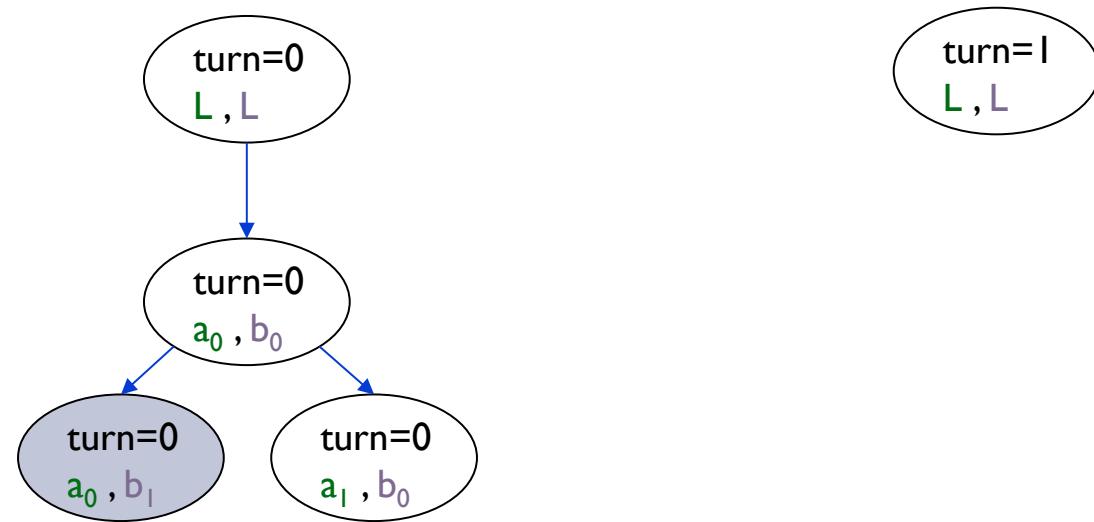
Pb:
b0: while True do
    b1: wait (turn = 1)
    b2: turn = 0
    end while
```



# Software Model Checking

```
Pa
a0: while True do
    a1: wait (turn = 0)
    a2: turn = 1
    end while

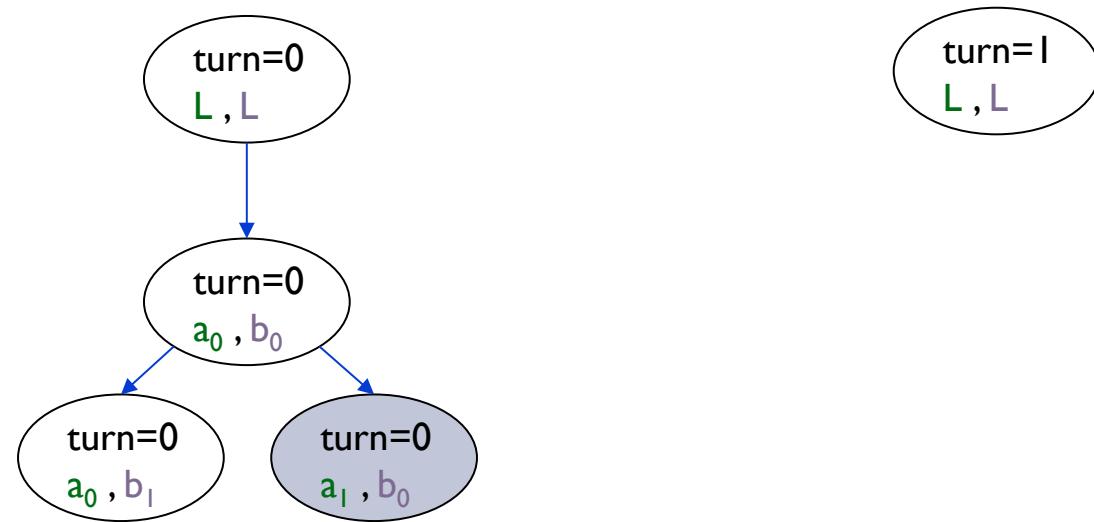
Pb:
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    b1: wait (turn = 1)
    b2: turn = 0
    end while
```



# Software Model Checking

```
Pa
a0: while True do
a1:   wait (turn = 0)
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Pb:
b0: while True do
b1:   wait (turn = 1)
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         end while
```



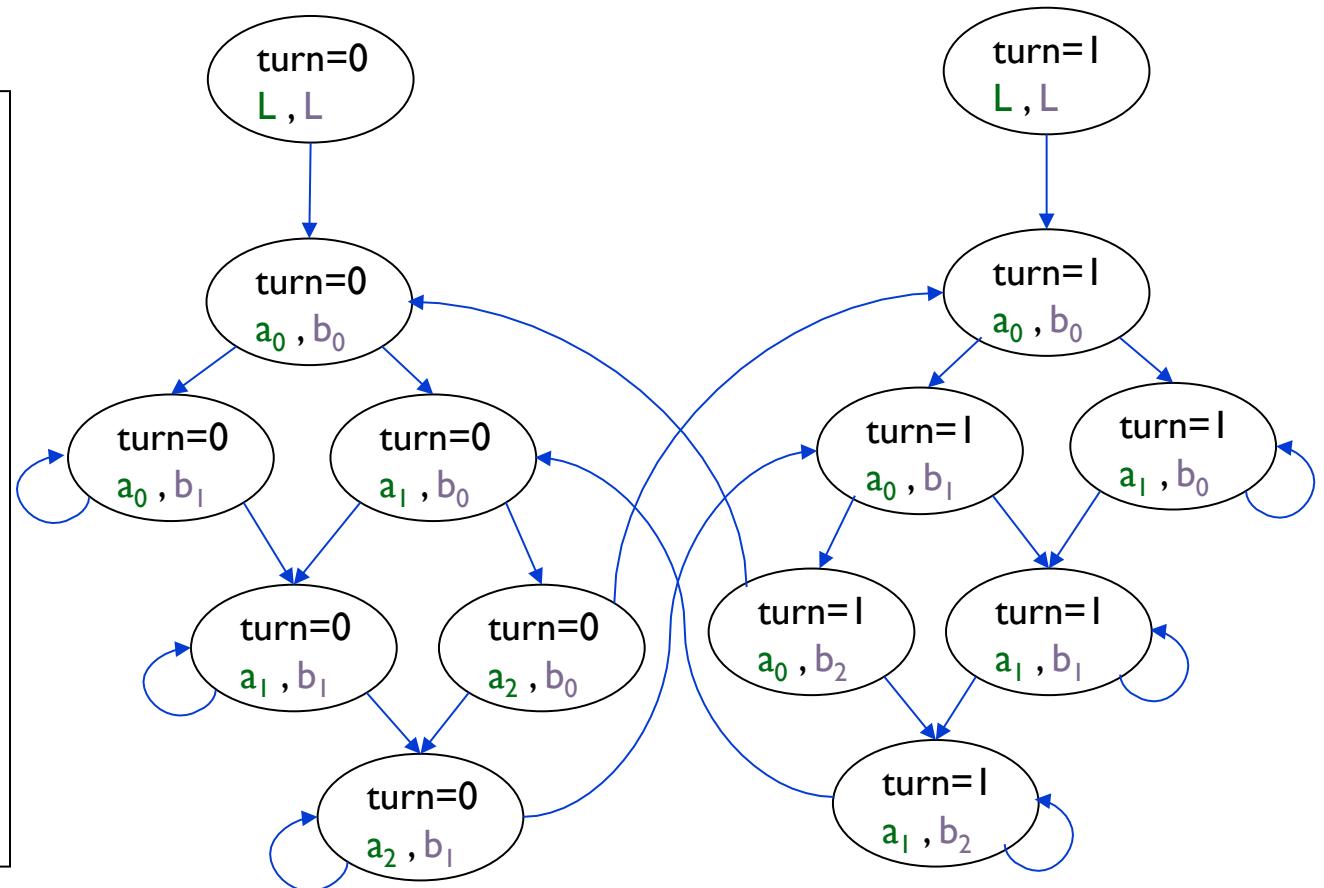
# Software Model Checking

$P_a$

```
a0: while True do  
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end while
```

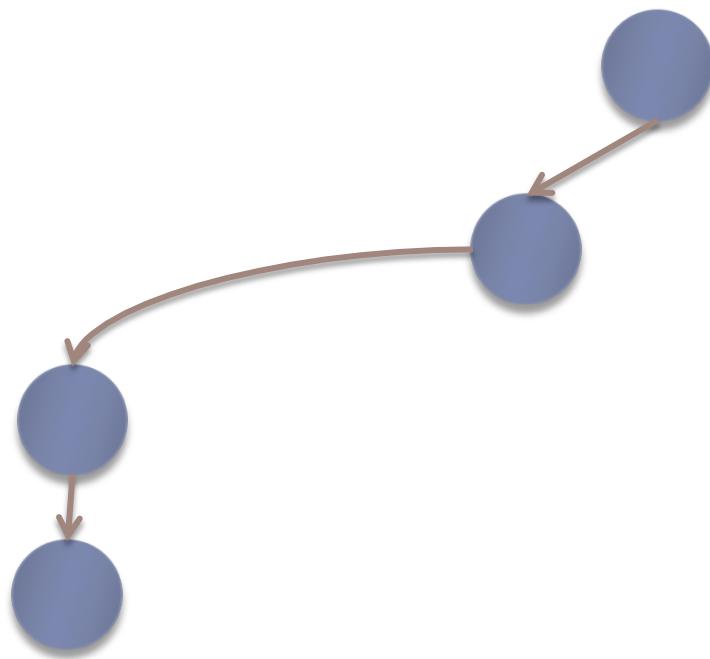
$P_b$ :

```
b0: while True do  
b1:   wait (turn = 1)  
b2:   turn = 0  
end while
```

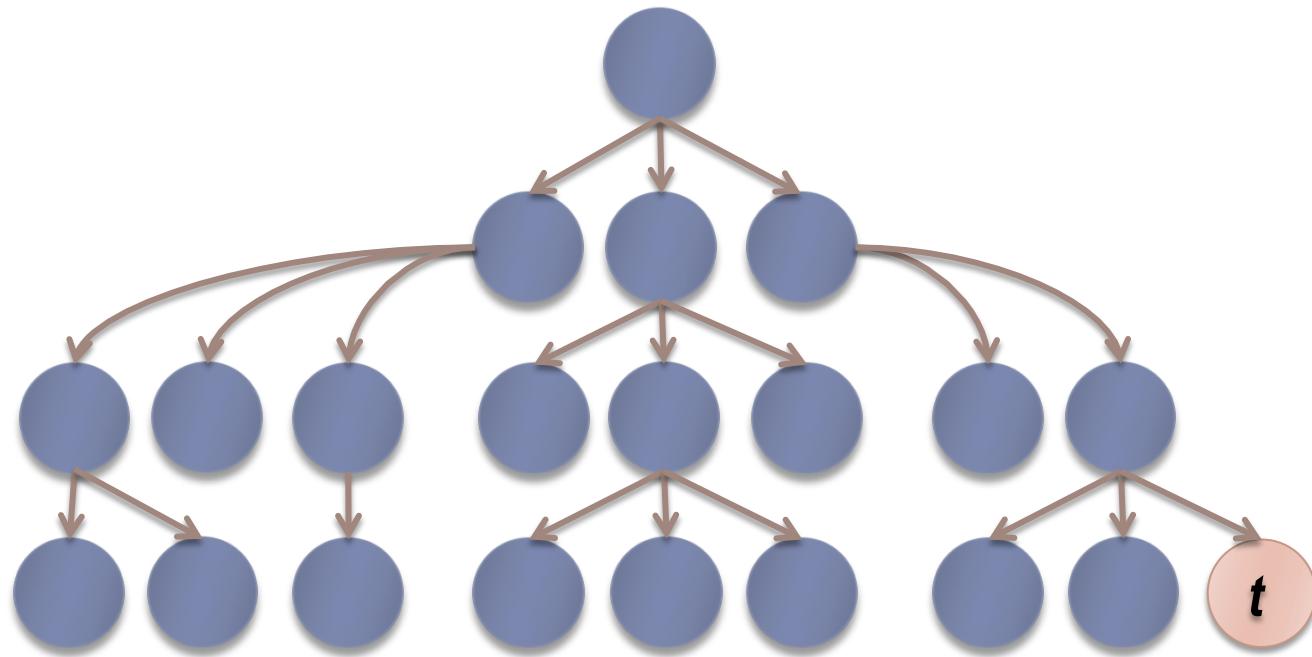


# Depth-first search

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# Depth-first search



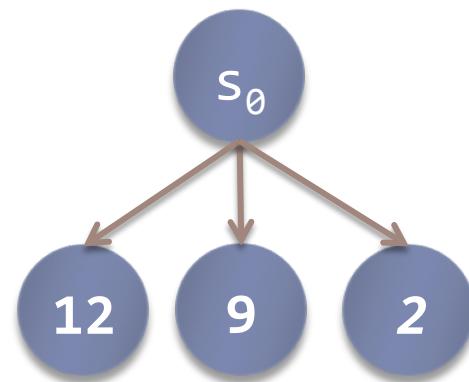
# Guided Search

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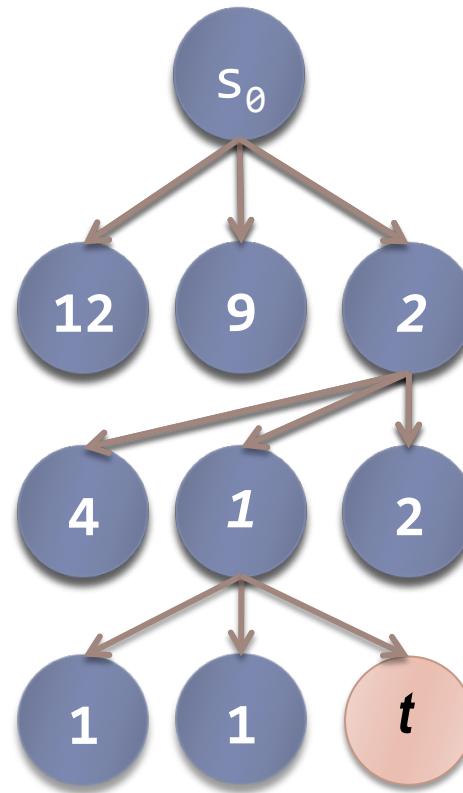


# Guided Search

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# Guided Search



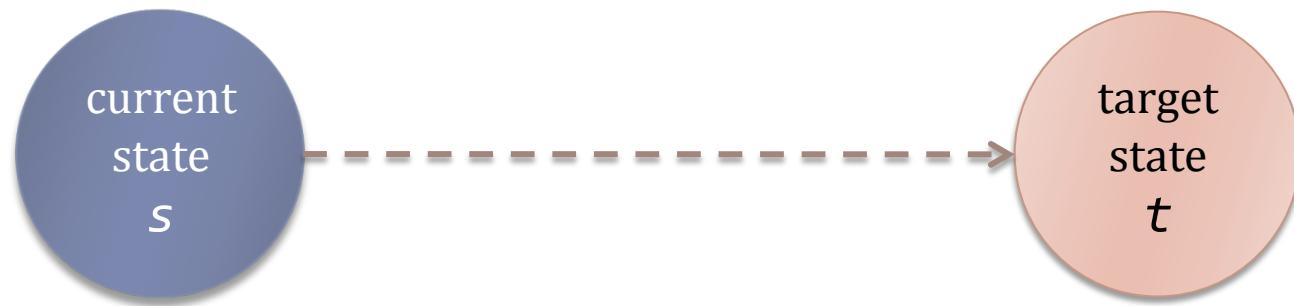
# How to Compute the Heuristic

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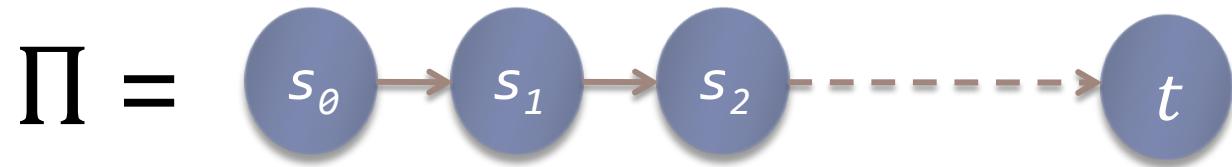
# Distance to Target

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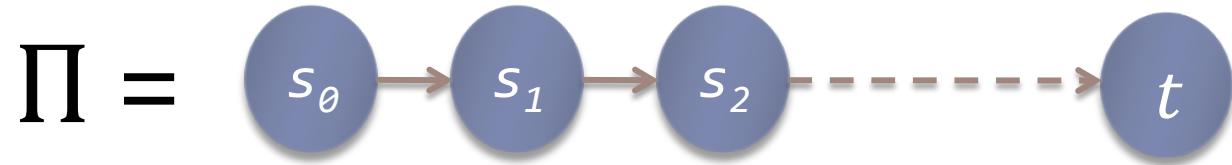
# Distance to Target

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# Distance to Target

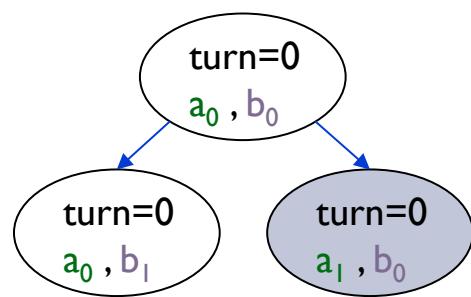
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Actual Distance:  
 $d(s_0, t) = |\pi|$

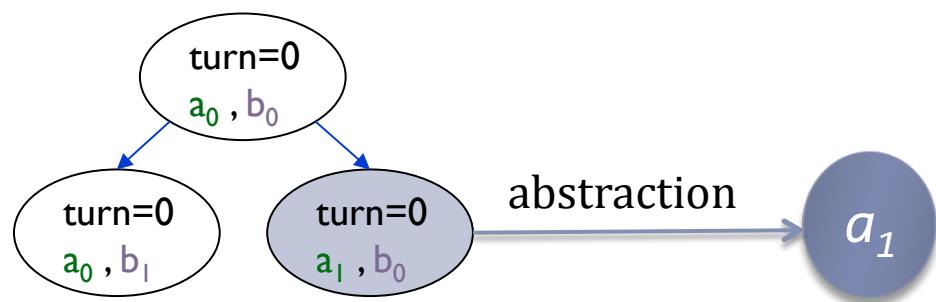
# Abstraction

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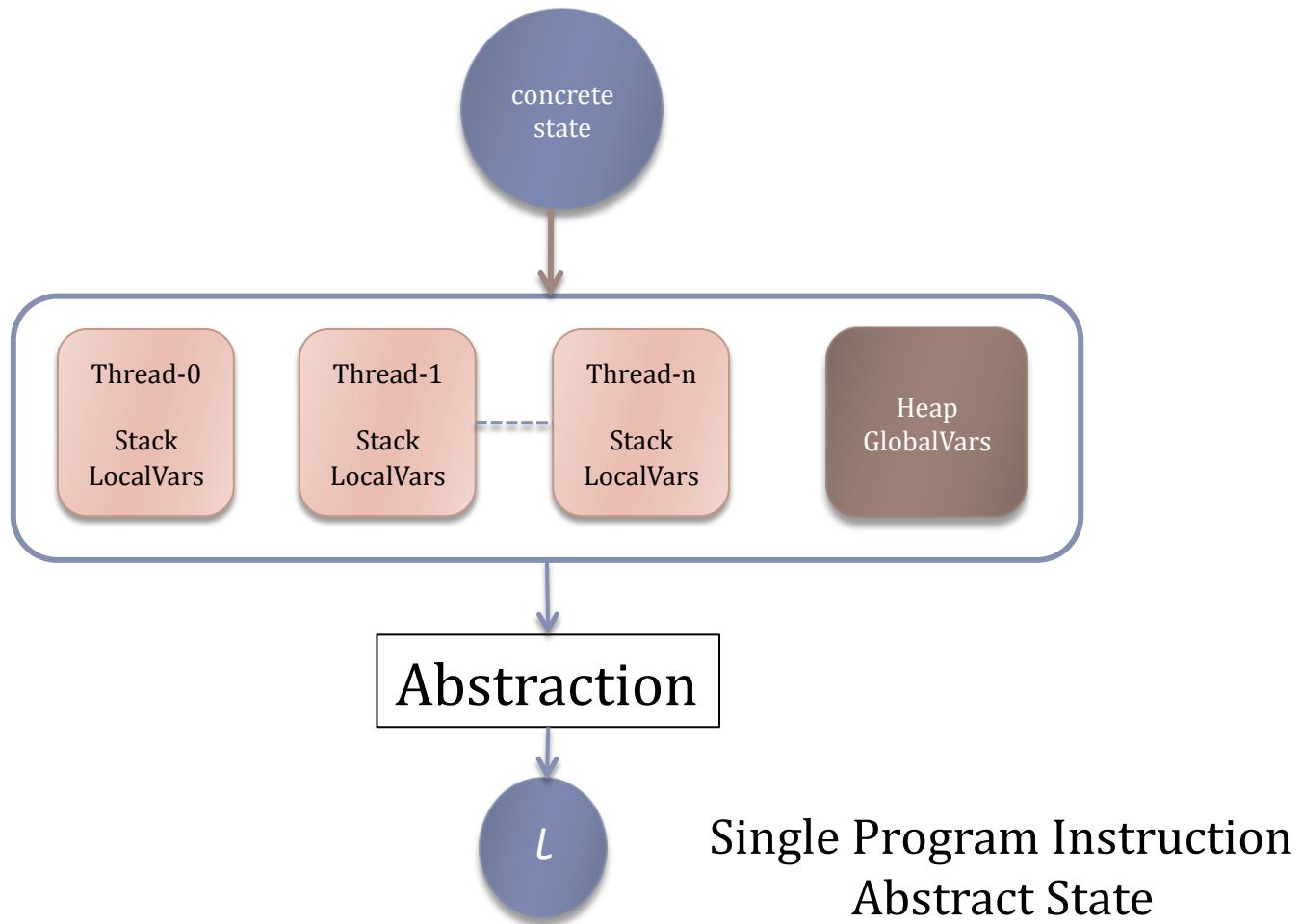


# Abstraction

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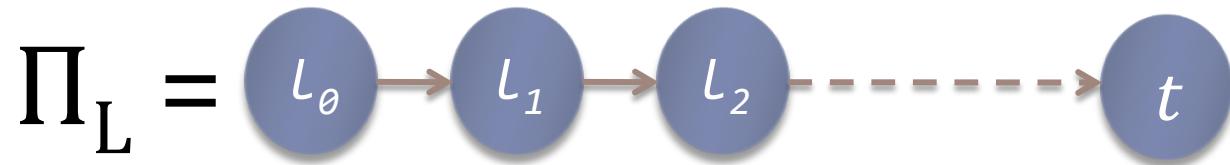


# Abstraction



# Heuristic: An Estimation

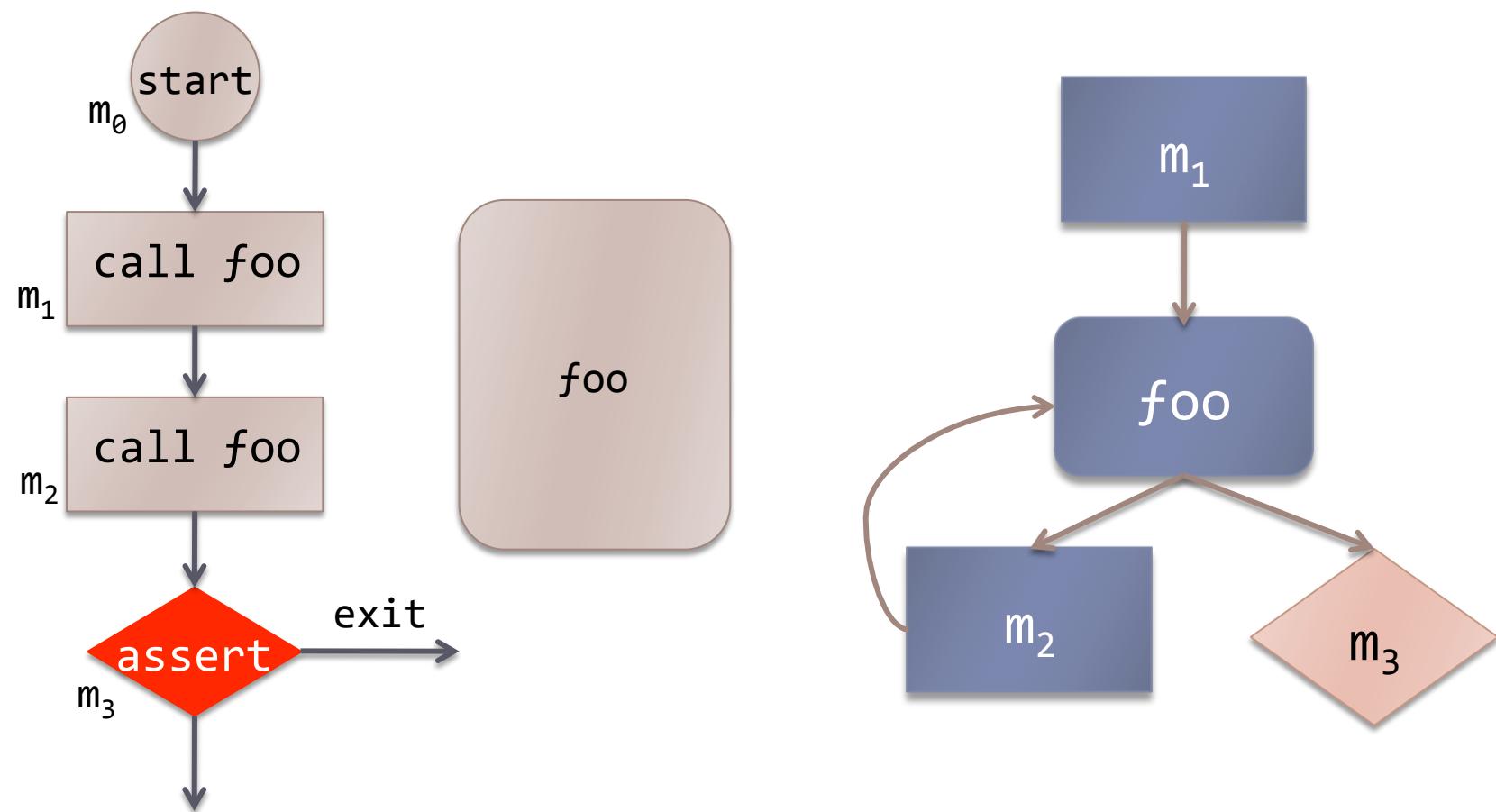
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Estimated Distance:

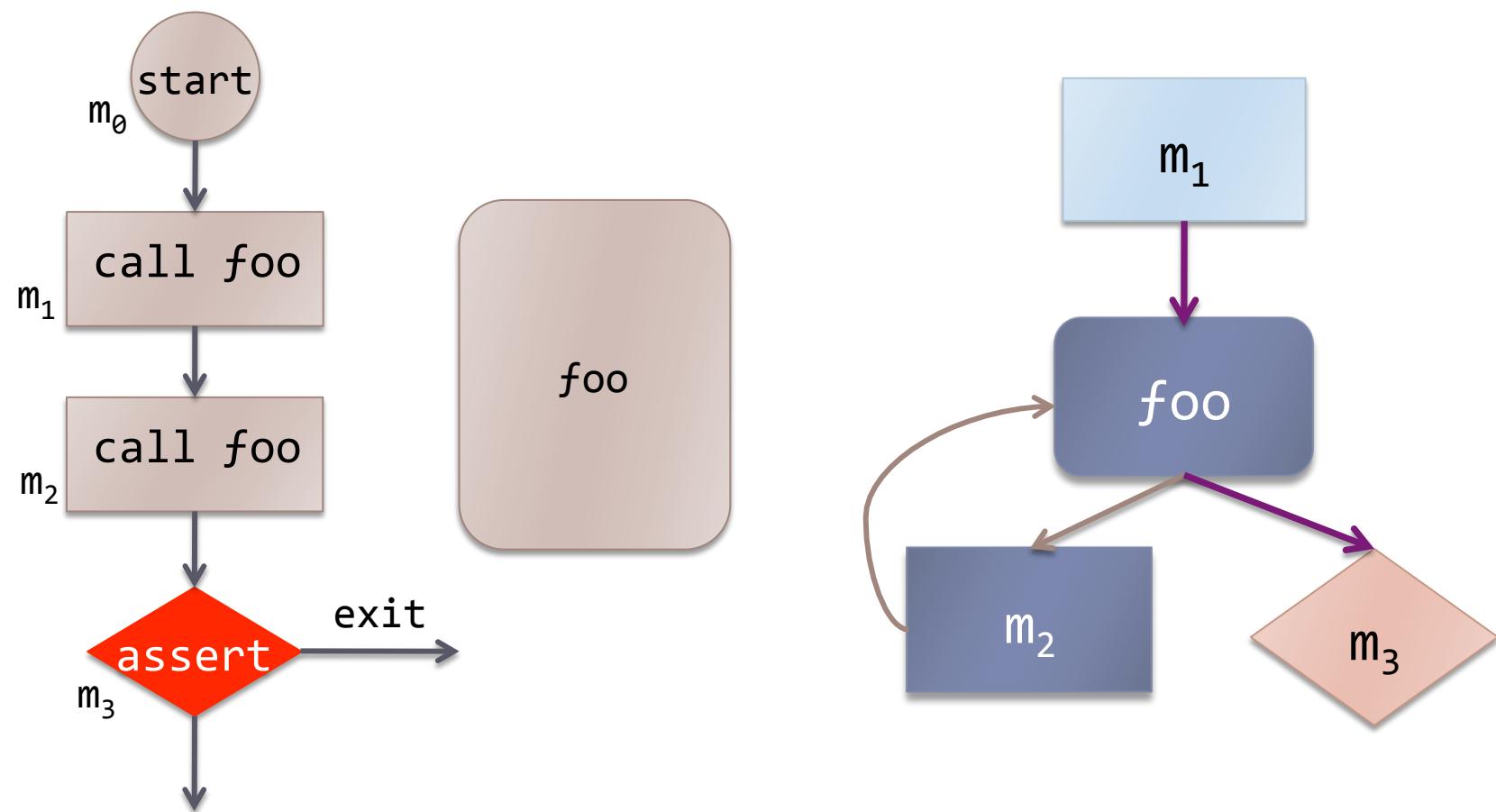
$$h(l, t) = |\pi|$$

# FSM Distance Heuristic



(Edelkamp & Mehler 2003)

# FSM Distance Heuristic



(Edelkamp & Mehler 2003)

# Motivation

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- ▶ Increasing use of Java and C#
- ▶ Inherently encourage use of Polymorphism
- ▶ Used to develop concurrent applications
- ▶ JDK Concurrent Library
- ▶ Dynamic Method Invocation
- ▶ Cannot resolve types statically

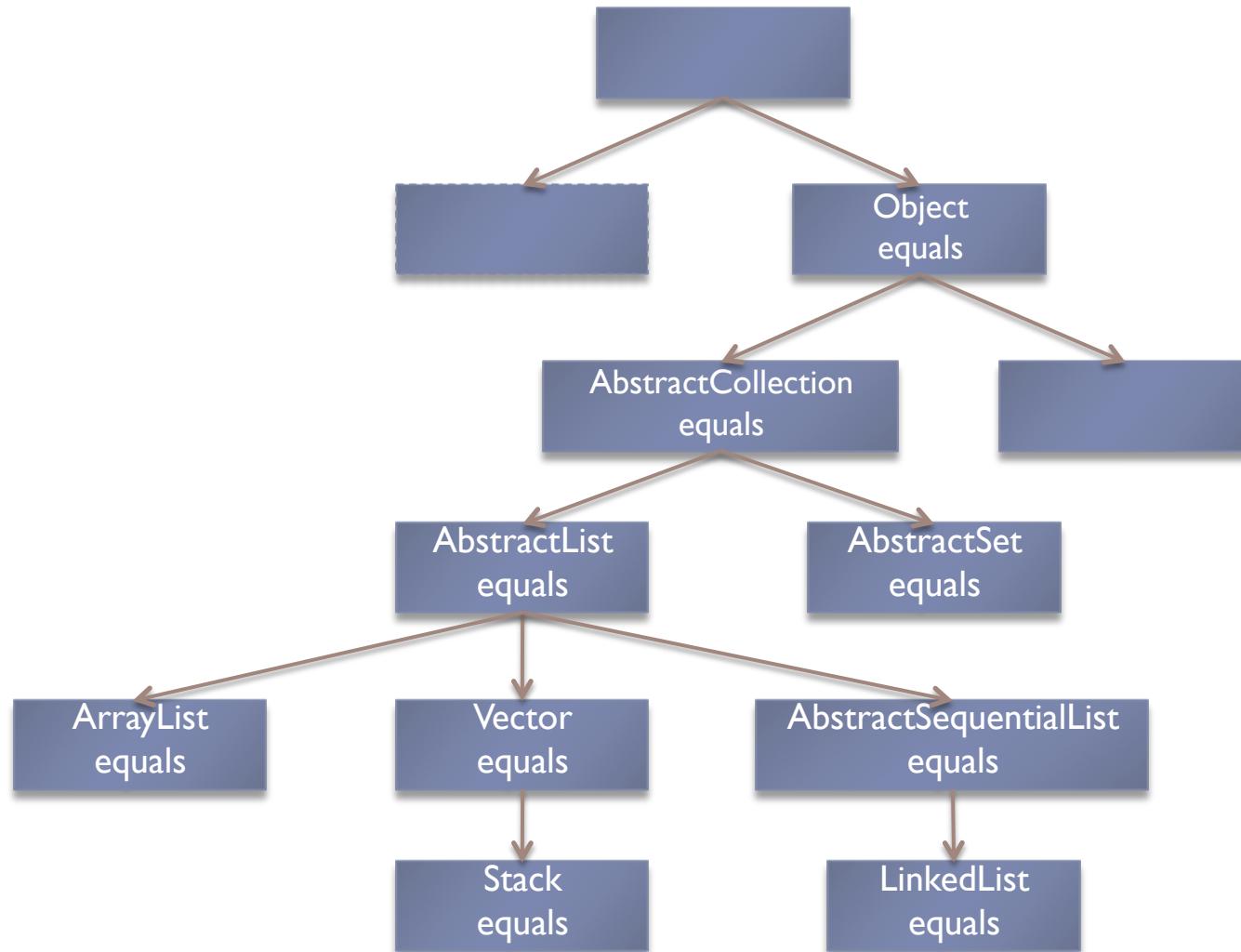
# Motivation

```
class AbstractList implements List{  
    ...  
    public boolean equals (Object o) {  
l_0: if o == this then  
l_1:     return true;  
l_2: if !(o instanceof List) then  
l_3:     return false;  
l_4: ListIterator x:= ListIterator();  
l_5: ListIterator y:= (List o).listIterator();  
l_6: while x.hasNext() and y.hasNext()  
l_7:     Object o1 := x.next();  
l_8:     Object o2 := y.next();  
l_9:     if !(o1 == null ? o2 == null : o1.equals(o2)) then  
l10:         return false;  
l11: return !(x.hasNext() || y.hasNext())  
    }  
}
```

# Motivation

```
class AbstractList implements List{  
    ...  
    public boolean equals (Object o) {  
        l0: if o == this then  
        l1:     return true;  
        l2: if !(o instanceof List) then  
        l3:     return false;  
        l4: ListIterator x:= ListIterator();  
        l5: ListIterator y:= (List o).listIterator();  
        l6: while x.hasNext() and y.hasNext()  
        l7:     Object o1 := x.next();  
        l8:     Object o2 := y.next();  
        l9:     if !(o1 == null ? o2 == null : o1.equals(o2)) then  
        l10:         return false;  
        l11: return !(x.hasNext() || y.hasNext())  
    }  
}
```

# Motivation

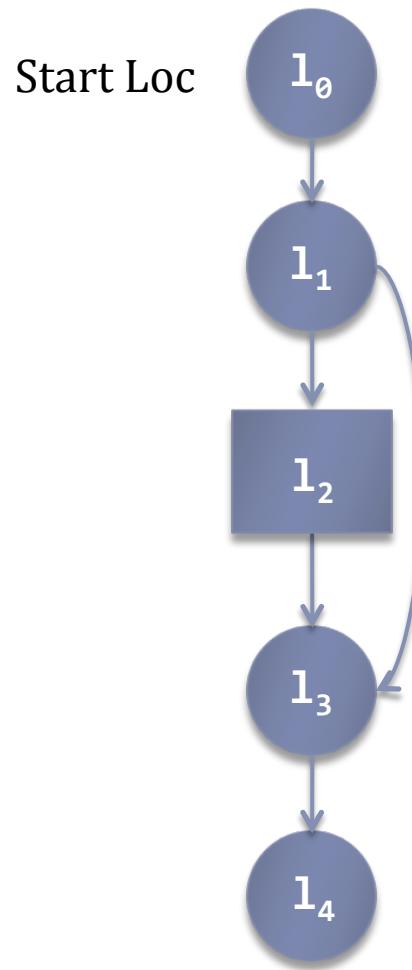


# Polymorphic Distance Heuristic (PFSM)

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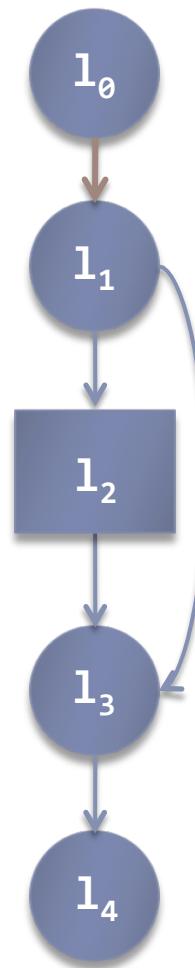
- ▶ Static Analysis Phase
- ▶ Compute a lower-bound
- ▶ Dynamic Heuristic Computation
- ▶ Use runtime information to resolve types
- ▶ Refine distance estimates

# Static Analysis Phase



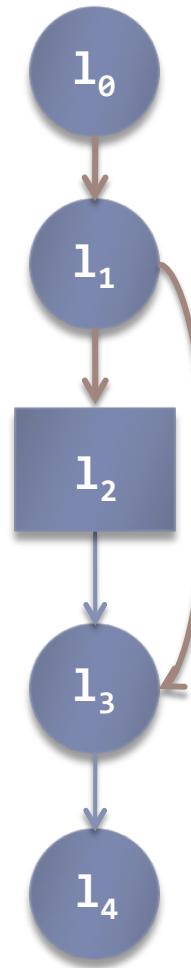
	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	$\infty$	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	$\infty$	$\infty$	$\infty$
$l_2$	$\infty$	$\infty$	0	$\infty$	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Static Analysis Phase



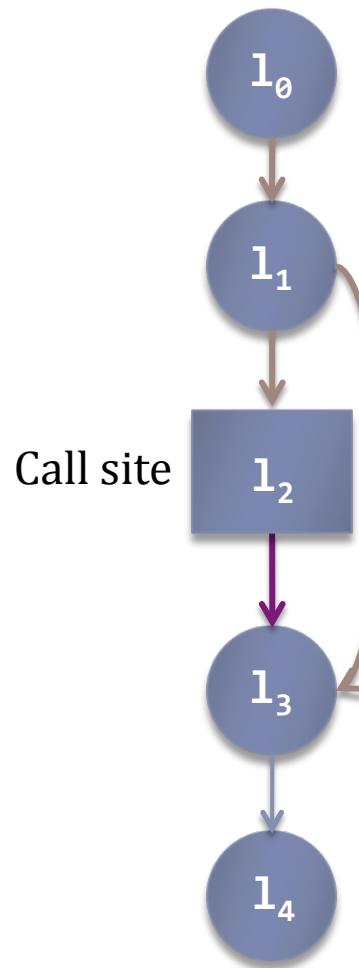
	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	$\infty$	$\infty$	$\infty$
$l_2$	$\infty$	$\infty$	0	$\infty$	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Static Analysis Phase



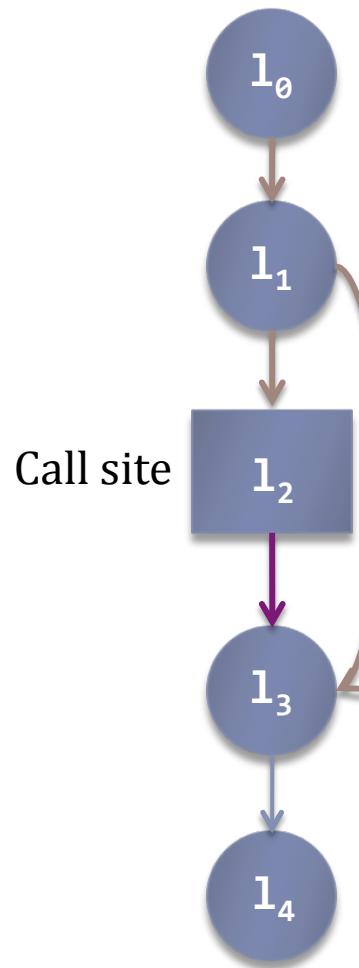
	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	1	1	$\infty$
$l_2$	$\infty$	$\infty$	0	$\infty$	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Static Analysis Phase



	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	1	1	$\infty$
$l_2$	$\infty$	$\infty$	0	$\infty$	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Static Analysis Phase



	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	1	1	$\infty$
$l_2$	$\infty$	$\infty$	0	$\infty$	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

Case 1: The target of the call site is resolved

# Reverse Invocation Order



	$l_5$	$l_6$	$l_7$
$l_5$	0	$\infty$	$\infty$
$l_6$	$\infty$	0	$\infty$
$l_7$	$\infty$	$\infty$	0

# Reverse Invocation Order



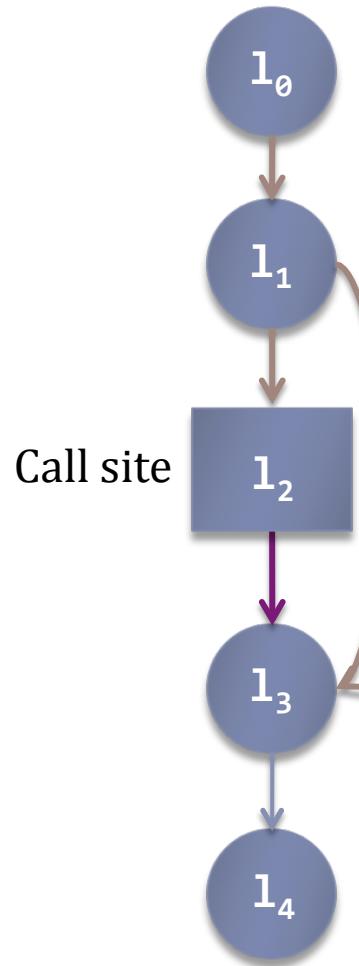
	$l_5$	$l_6$	$l_7$
$l_5$	0	1	$\infty$
$l_6$	$\infty$	0	1
$l_7$	$\infty$	$\infty$	0

# Reverse Invocation Order



	$l_5$	$l_6$	$l_7$
$l_5$	0	1	2
$l_6$	$\infty$	0	1
$l_7$	$\infty$	$\infty$	0

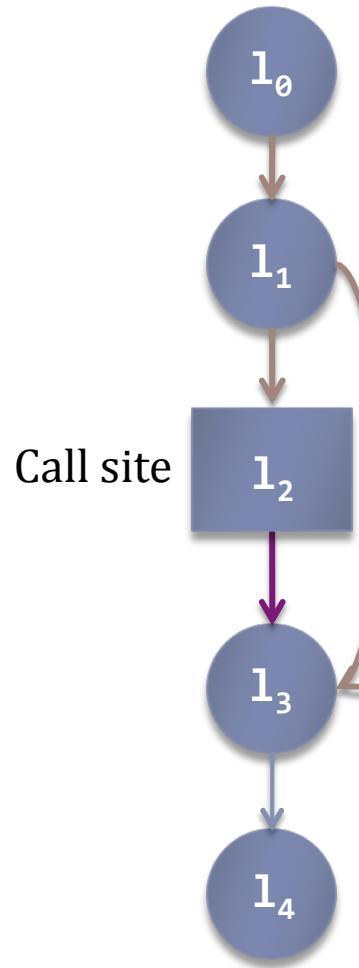
# Static Analysis Phase



	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	1	1	$\infty$
$l_2$	$\infty$	$\infty$	0	<b>2+2</b>	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

Case 1: The target of the call site is resolved

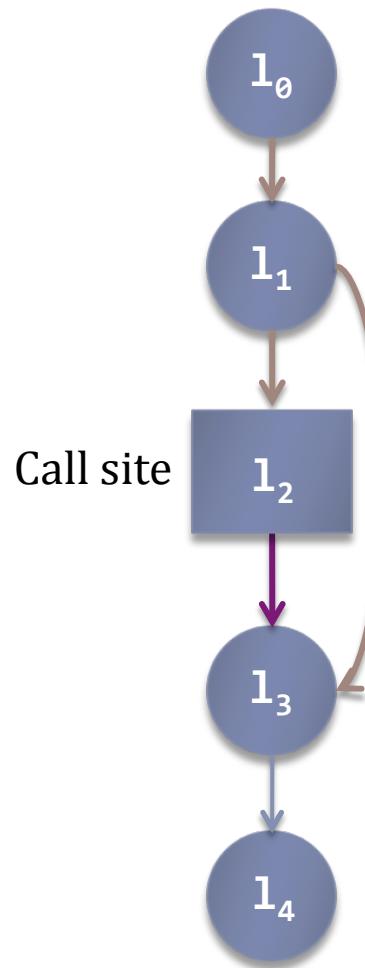
# Static Analysis Phase



	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	1	1	$\infty$
$l_2$	$\infty$	$\infty$	0	$\infty$	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

Case 2: The target of the call site is not resolved

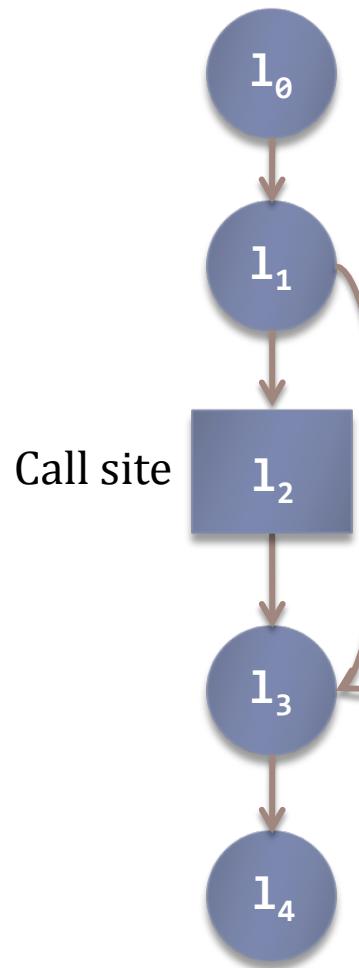
# Static Analysis Phase



	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	$\infty$	$\infty$	$\infty$
$l_1$	$\infty$	0	1	1	$\infty$
$l_2$	$\infty$	$\infty$	0	2	$\infty$
$l_3$	$\infty$	$\infty$	$\infty$	0	$\infty$
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

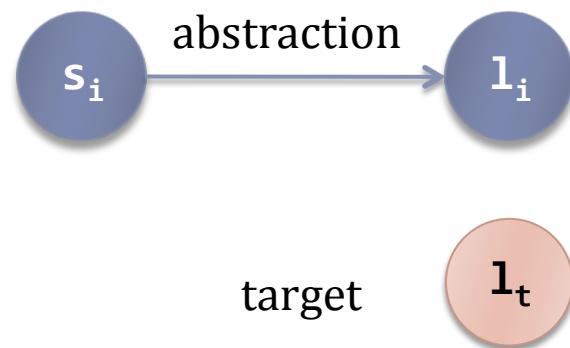
Case 2: The target of the call site is not resolved

# Static Analysis Phase



	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	2	2	3
$l_1$	$\infty$	0	1	1	2
$l_2$	$\infty$	$\infty$	0	2	3
$l_3$	$\infty$	$\infty$	$\infty$	0	1
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Assigning Heuristic Values



Current Location:  $l_i$

Target location:  $l_t$

# Dynamic Heuristic Computation

Current Location:  $l_i == l_0$

Target location:  $l_t == l_3$

	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	2	2	3
$l_1$	$\infty$	0	1	1	2
$l_2$	$\infty$	$\infty$	0	2	3
$l_3$	$\infty$	$\infty$	$\infty$	0	1
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Dynamic Heuristic Computation

Current Location:  $l_i == l_0$

Target location:  $l_t == l_3$

	$l_0$	$l_1$	$l_2$	$l_3$	$l_4$
$l_0$	0	1	2	2	3
$l_1$	$\infty$	0	1	1	2
$l_2$	$\infty$	$\infty$	0	2	3
$l_3$	$\infty$	$\infty$	$\infty$	0	1
$l_4$	$\infty$	$\infty$	$\infty$	$\infty$	0

# Dynamic Heuristic Computation

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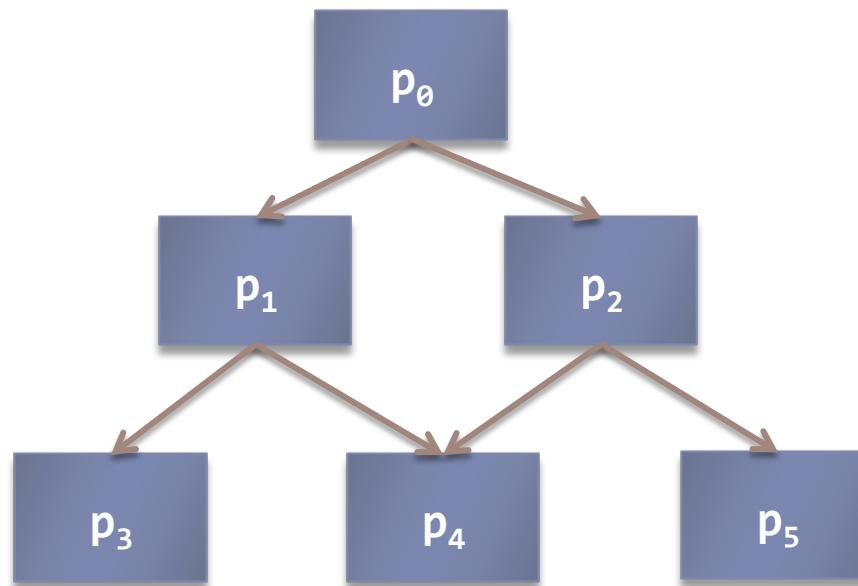
Current Location:  $l_i == l_1$

Target location:  $l_t == l_{18}$

# Dynamic Heuristic Computation

Current Location:  $l_i == l_1$

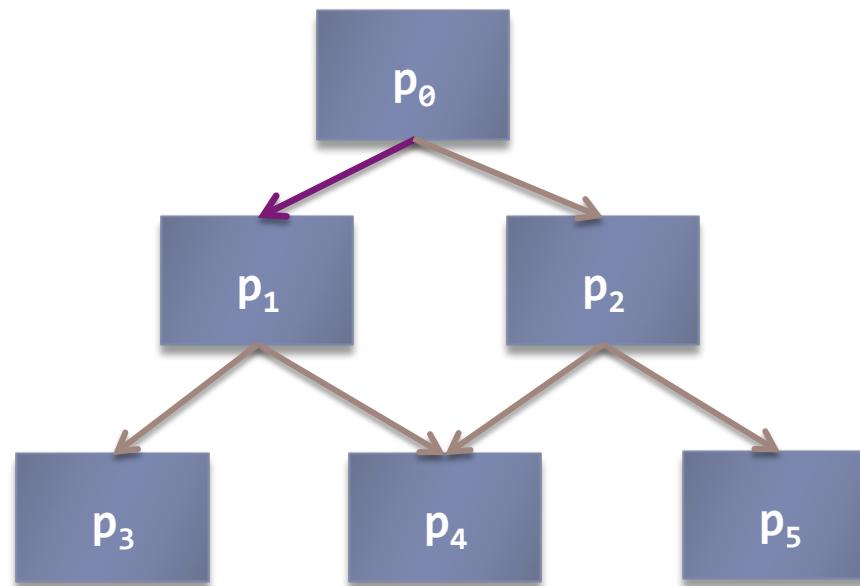
Target location:  $l_t == l_{18}$



# Dynamic Heuristic Computation

Current Location:  $l_i == l_1$

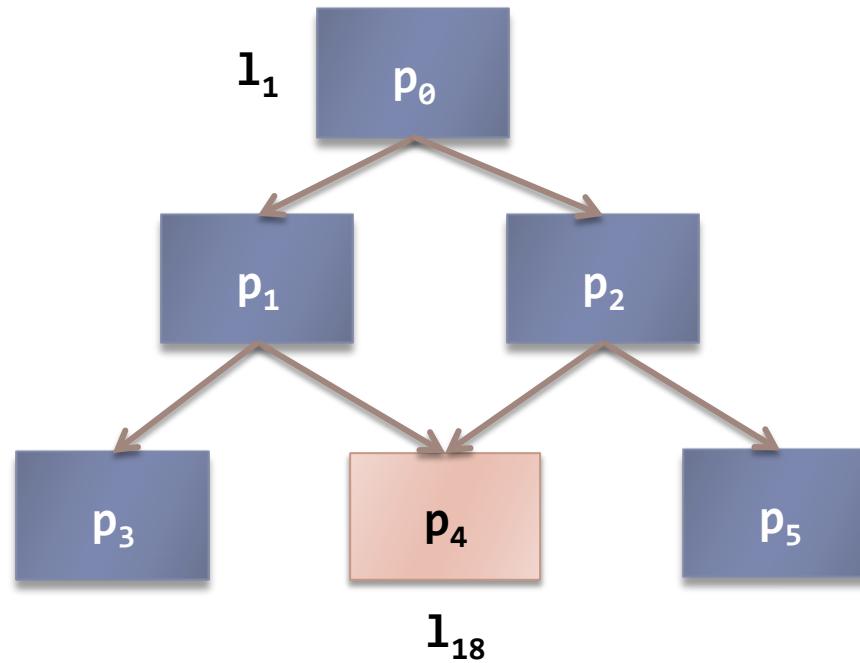
Target location:  $l_t == l_{18}$



# Dynamic Heuristic Computation

Current Location:  $l_i == l_1$

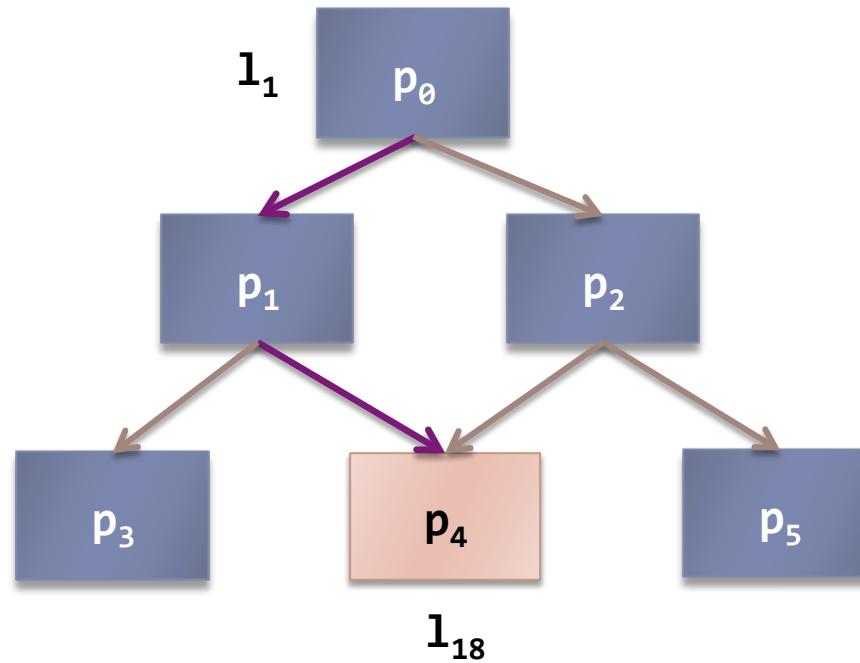
Target location:  $l_t == l_{18}$



# Dynamic Heuristic Computation

Current Location:  $l_i == l_1$

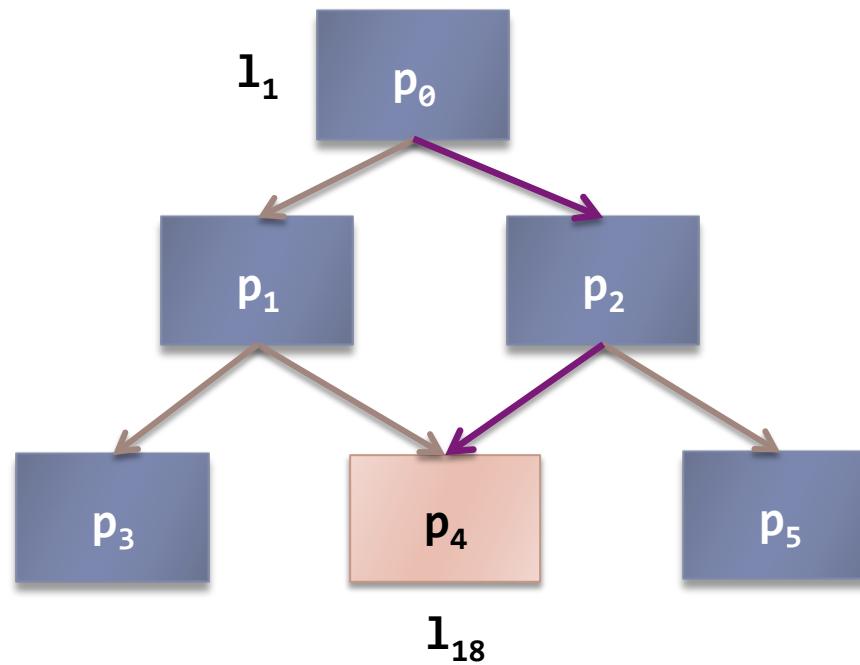
Target location:  $l_t == l_{18}$



# Dynamic Heuristic Computation

Current Location:  $l_i == l_1$

Target location:  $l_t == l_{18}$



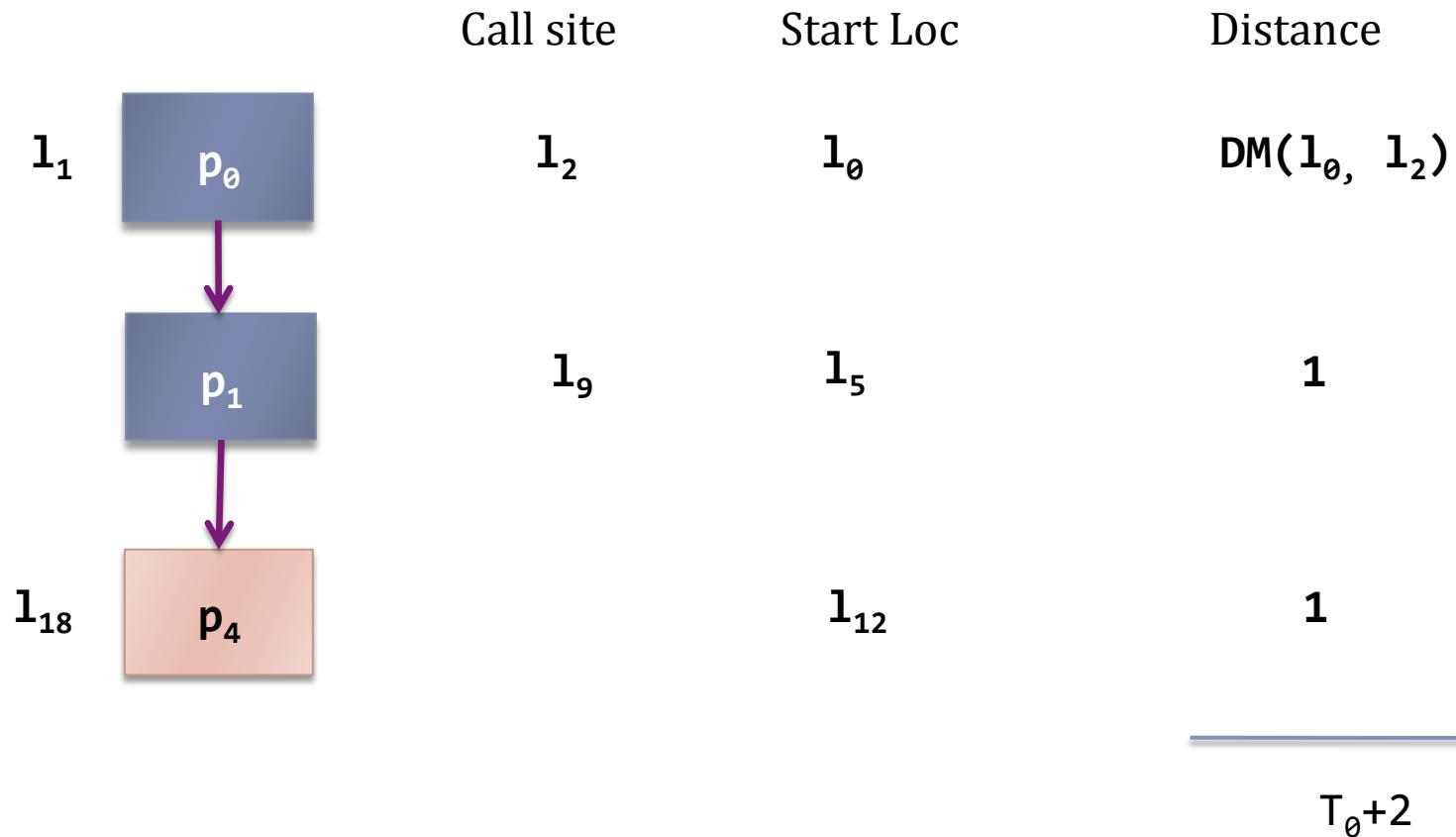
# Dynamic Heuristic Computation

	Call site	Start Loc	Distance
$l_1$	$p_0$	$l_2$	$DM(l_1, l_2)$
		$l_9$	$DM(l_5, l_9)$
$l_{18}$	$p_4$	$l_{12}$	$DM(l_{12}, l_{18})$

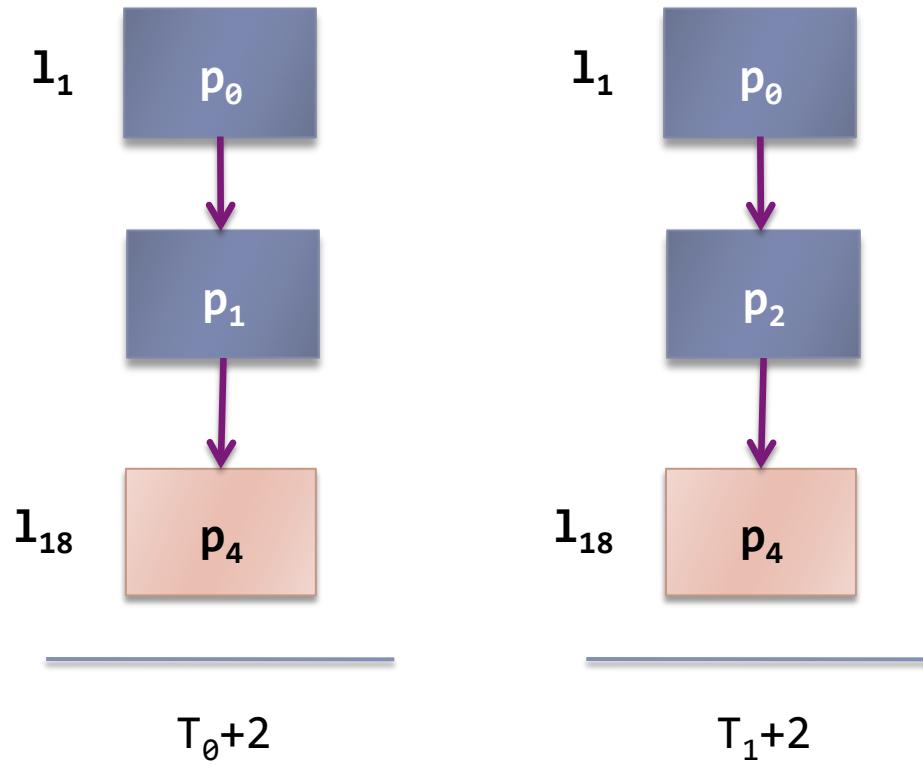
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$T_\theta + 2$

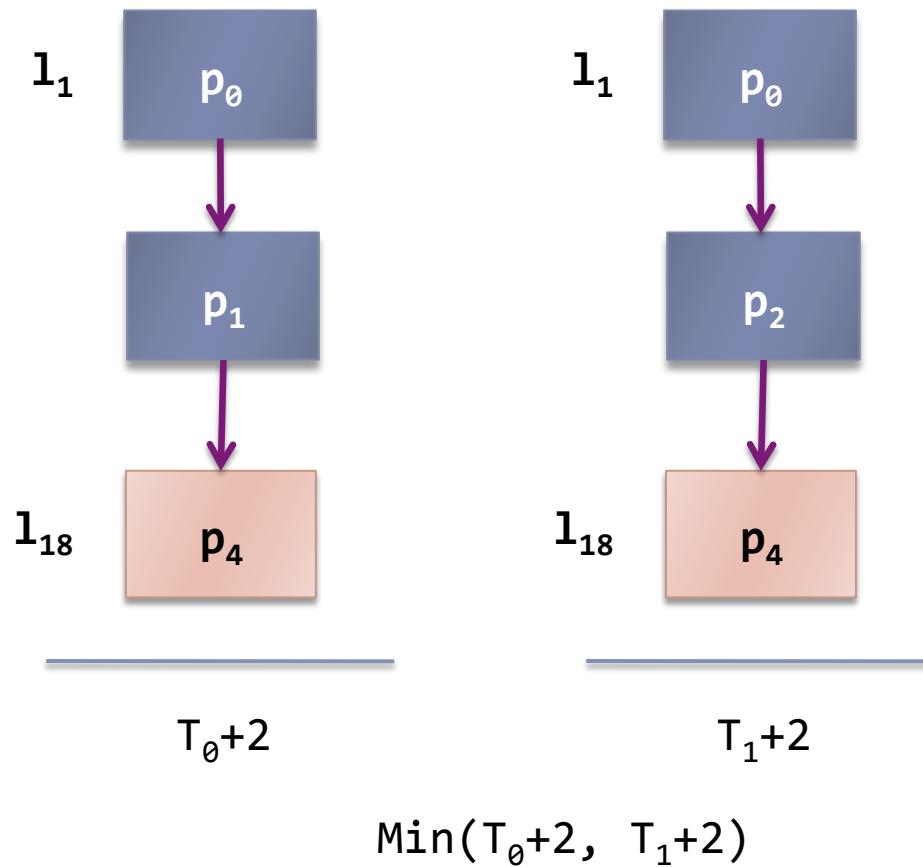
# Dynamic Heuristic Computation



# Dynamic Heuristic Computation



# Dynamic Heuristic Computation



# PFSM Distance Heuristic

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- ▶ Computes a lower bound on the distance estimate
- ▶ Admissible and Consistent
- ▶ In an A\* search optimal counter-example
- ▶ Lower Complexity than FSM distance heuristic
- ▶ Tighter lower-bound than FSM distance heuristic

# Empirical Evaluation

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- ◆ 100 Greedy depth-first trials
- ◆ Heuristic ties are randomly broken
- ◆ Time bound of 1 hour
- ◆ Consistent with other recent studies
- ◆ Use JPF model checker
- ◆ No data non-determinism
- ◆ 8 GB RAM and 2.6 GHz processor

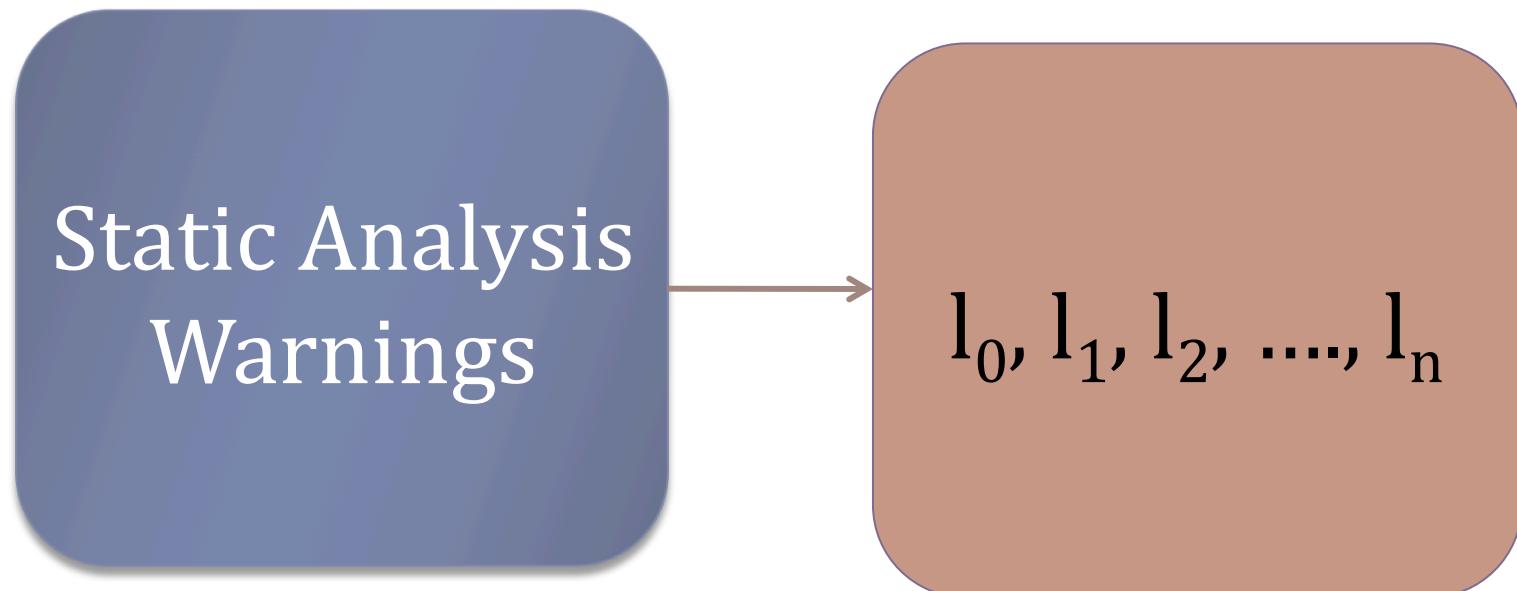


# Multi-threaded Java programs

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- ▶ TwoStage Benchmark  
SLOC: 52, Null Pointer Exception
- ▶ Reorder Benchmark  
SLOC: 44, Null Pointer Exception
- ▶ Wronglock Benchmark  
SLOC: 38, Deadlock
- ▶ AbsList Real JDK 1.4 concurrent library  
SLOC: 7267, Race in AbstractList class
- ▶ AryList Real JDK 1.4 concurrent library  
SLOC: 7169, Race in ArrayList class

# Generating Interesting Locations



# Avg. States Explored

Subject	Guided Search		
	PFSM	Random	FSM
TwoStage(7,1)	213	109,259	30,193
TwoStage(8,1)	251	204,790	46,259
TwoStage(10,1)	335	364,859	156,697
WrongLock(1,10)	3,781	7,064	196
Reorder(8,1)	197	34,193	24,022
AryList(1,10)	5,216	15,972	-
AbsList(1,10)	982	10,497,302	-

Average states generated in error discovering trials



# Avg. Total Time taken in Seconds

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Subject	Guided Search		
	PFSM	Random	FSM
TwoStage(7,1)	0.42	40.14	39.11
TwoStage(8,1)	0.41	76.24	41.87
TwoStage(10,1)	0.46	132.08	59.90
WrongLock(1,10)	1.66	2.85	10.70
Reorder(8,1)	0.39	9.70	13.90
AryList(1,10)	13.60	7.95	-
AbsList(1,10)	4.92	2585.79	-



# Related Work

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- ▶ Hamming Distance Heuristics  
(Yang & Dill 1998)
- ▶ Property-based Heuristics  
(Groce & Visser 2002)
- ▶ Trail-directed model checking  
(Edelkamp *et. al* 2001)
- ▶ Deterministic Execution technique  
(Harvey & Strooper 2001)
- ▶ Abstraction guided concrete execution  
(Nanshi & Somenzi 2006, Paula & Hu 2007)
- ▶ Concolic Testing  
(Sen *et. al* 2005; Sen & Agha 2007)

# Conclusions & Future work

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- ▶ Distance heuristic for programs with polymorphism
  - ▶ Conservative estimates in initial static analysis
  - ▶ Targets of dynamic method invocation resolved
  - ▶ Compute distance estimates with more information
  - ▶ PFSM outperforms Random and FSM Heuristic
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- ▶ Study trade-off between accuracy and performance
  - ▶ Propagate types to improve accuracy of PFSM heuristic

# Questions?

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