

# An Improved Distance Heuristic Function for Directed Software Model Checking

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# Motivation

- ◆ Use of embedded systems has become ubiquitous
- ◆ Growing complexity challenges ad-hoc testing methods
- ◆ Vector simulation finds bugs in the early design phase
- ◆ Code coverage techniques are not feasible
- ◆ Low-level scheduling decisions create concurrency errors
- ◆ Motivates a need for a formal approach to find these errors



# Software Model Checking

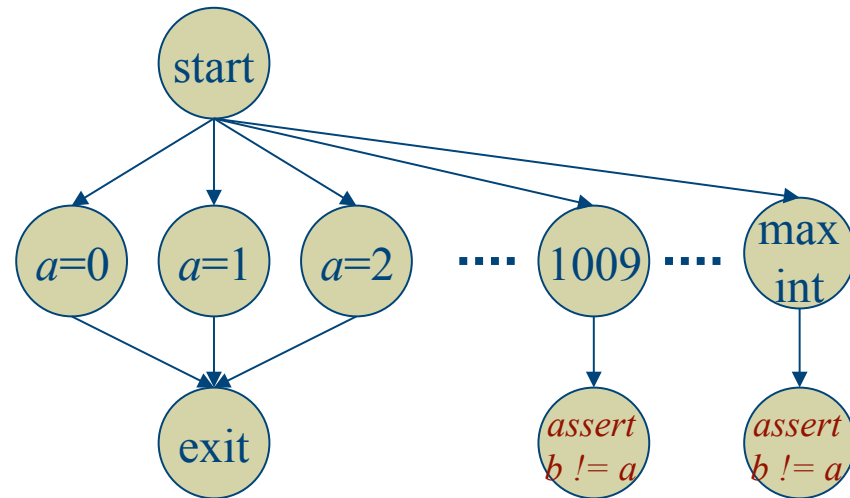
```
int b = 1009
void simple(){
  int a;
  read a;
  if (a > 1000)
    assert(b != a)
}
```

- ◆ It builds a model for a given software system



# Simple program

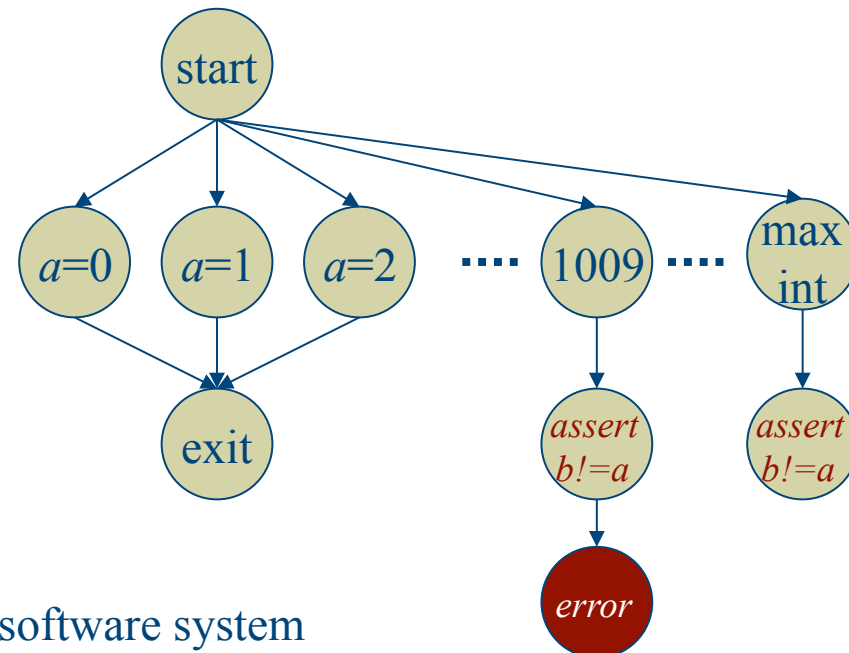
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- ◆ It builds a model for a given software system
- ◆ The transition graph represents all the behaviors of the system

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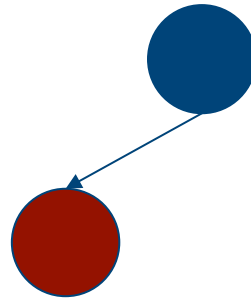


- ◆ It builds a model for a given software system
- ◆ The transition graph represents all the behaviors of the system
- ◆ The property being verified is whether there exists a path to the error

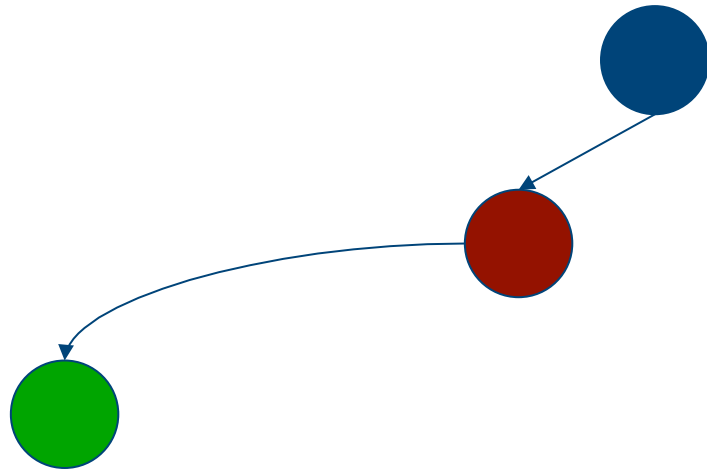
# Exhaustive Search - DFS



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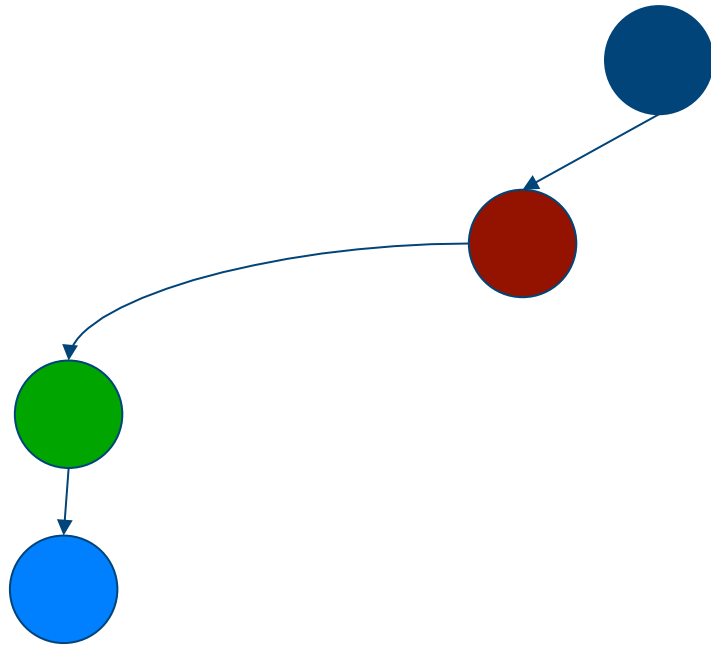


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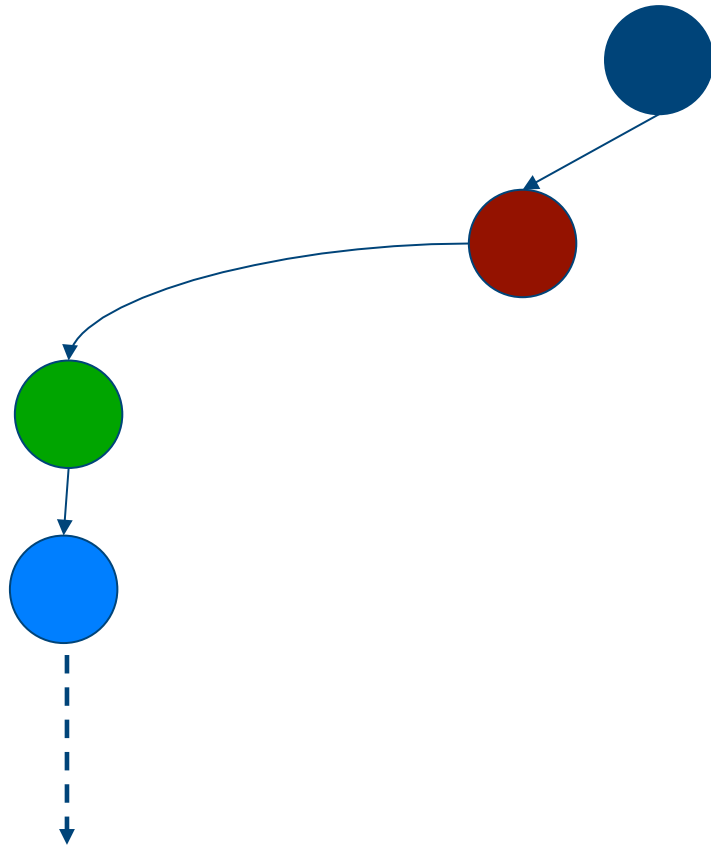




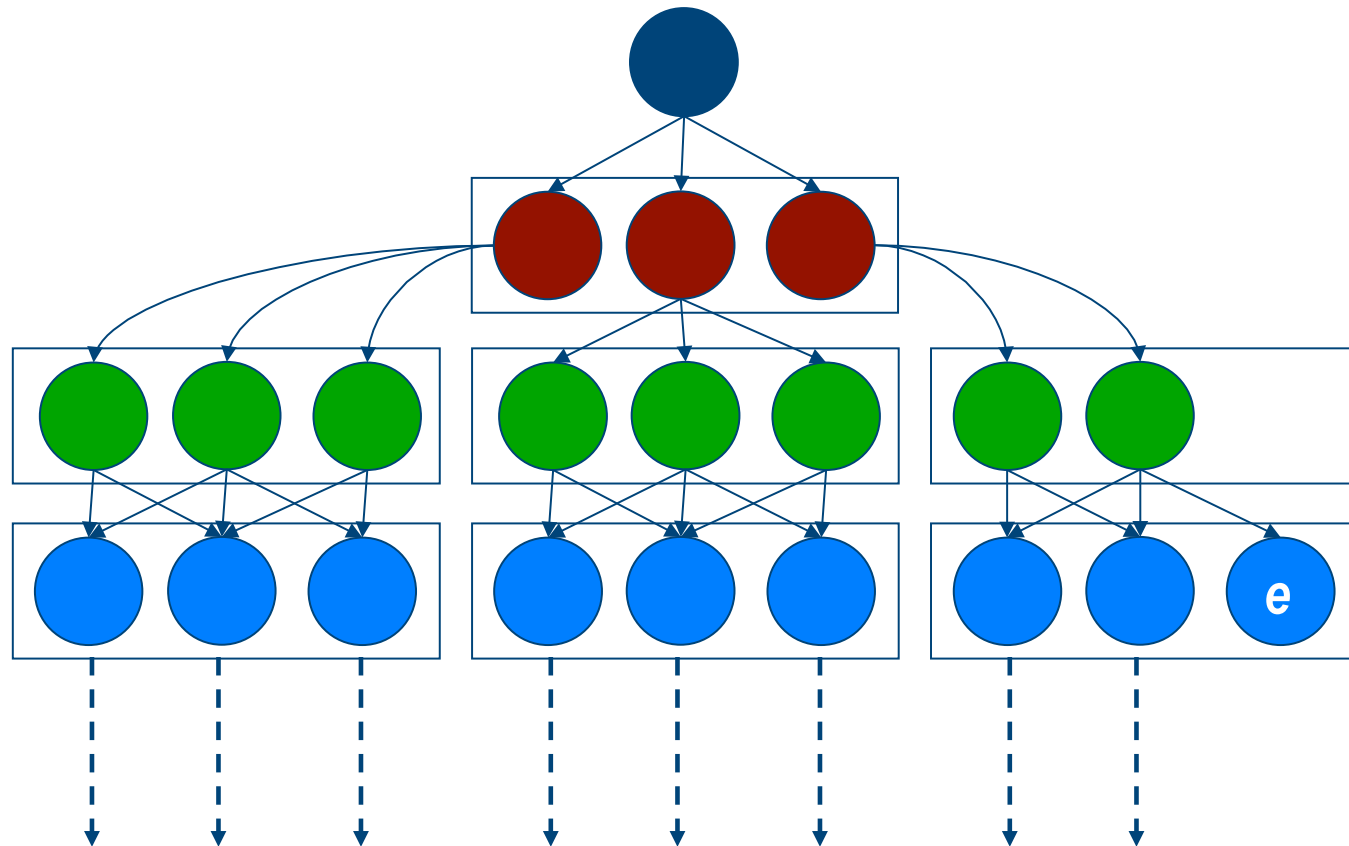
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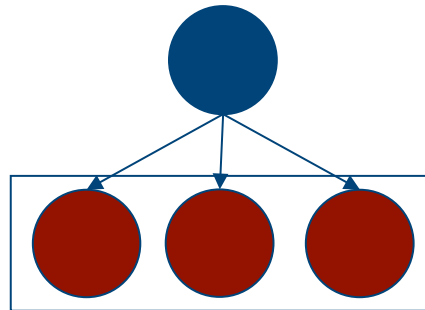
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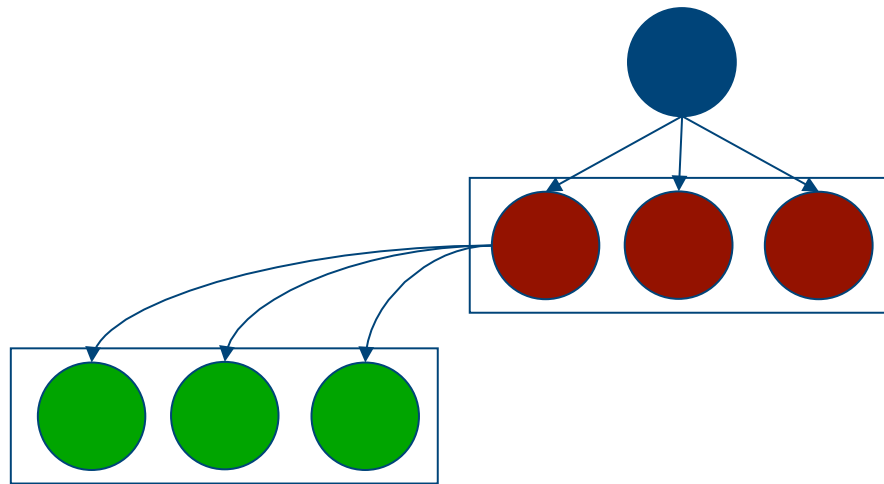
# Exhaustive Search - BFS



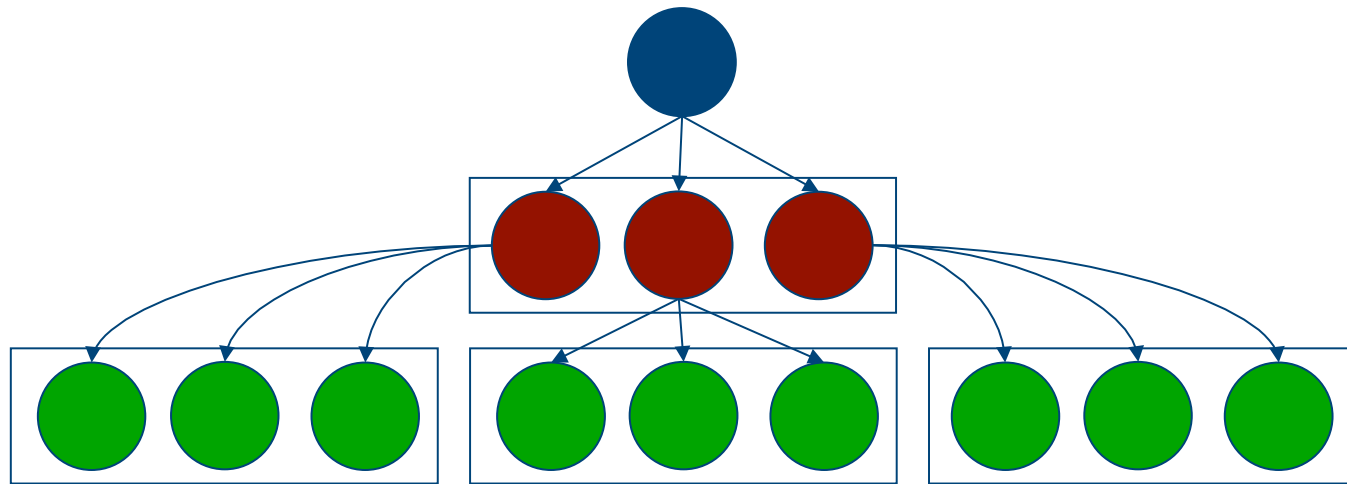
# Exhaustive Search - BFS



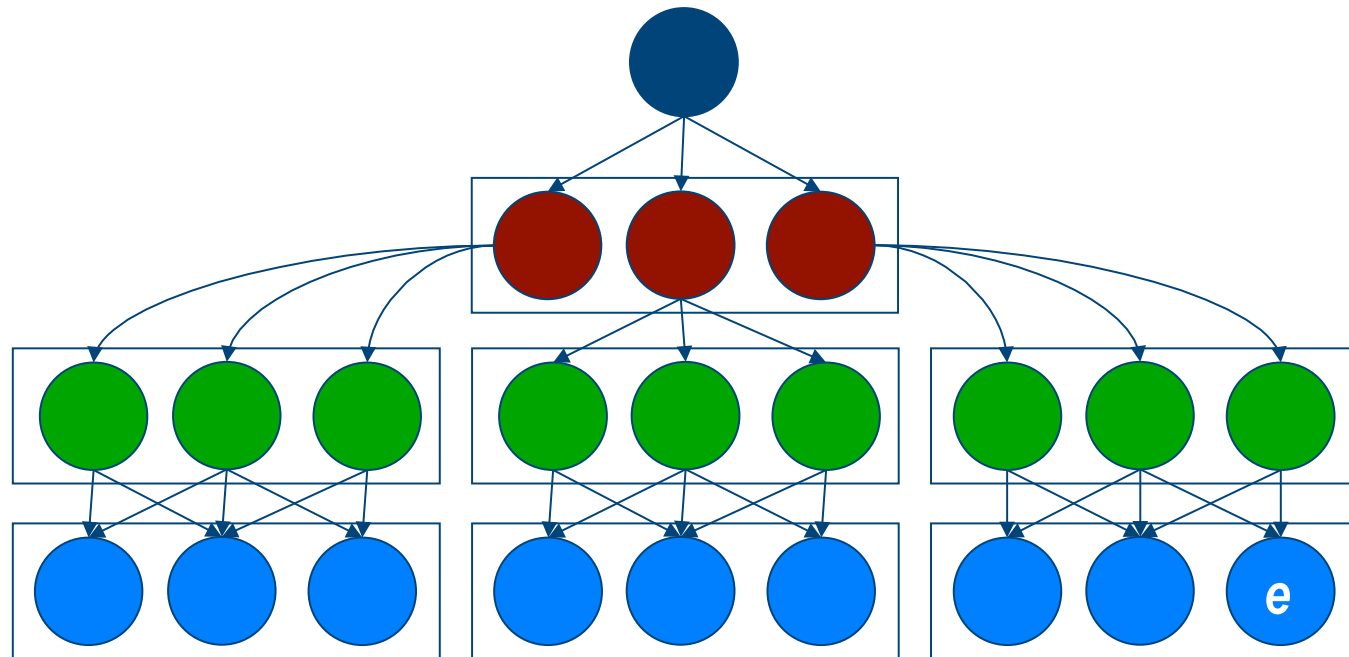
# Exhaustive Search - BFS



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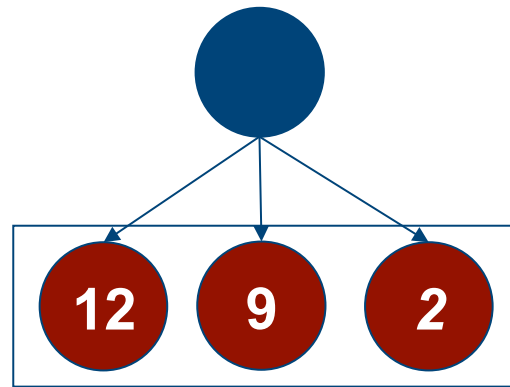




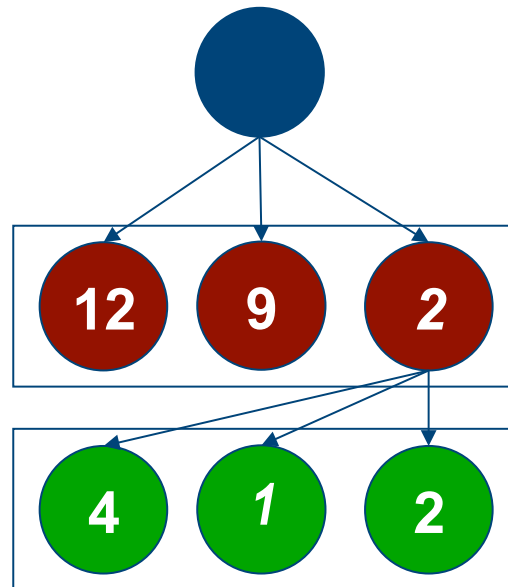
# Guided Best-first Search



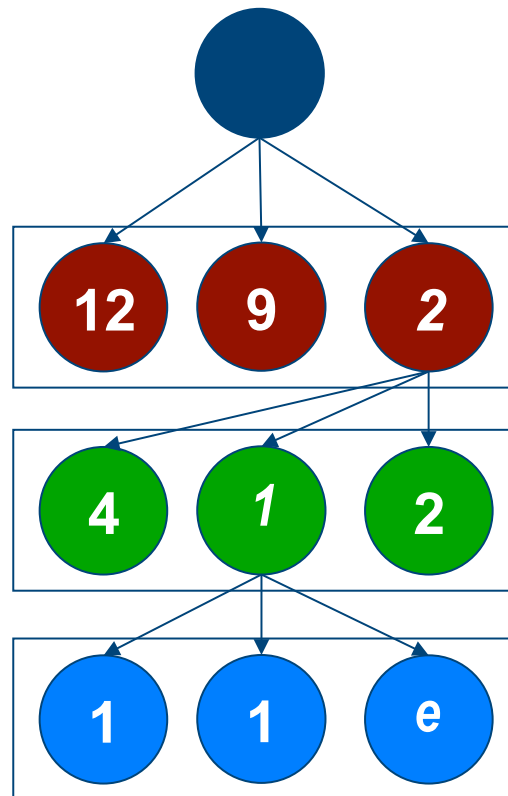
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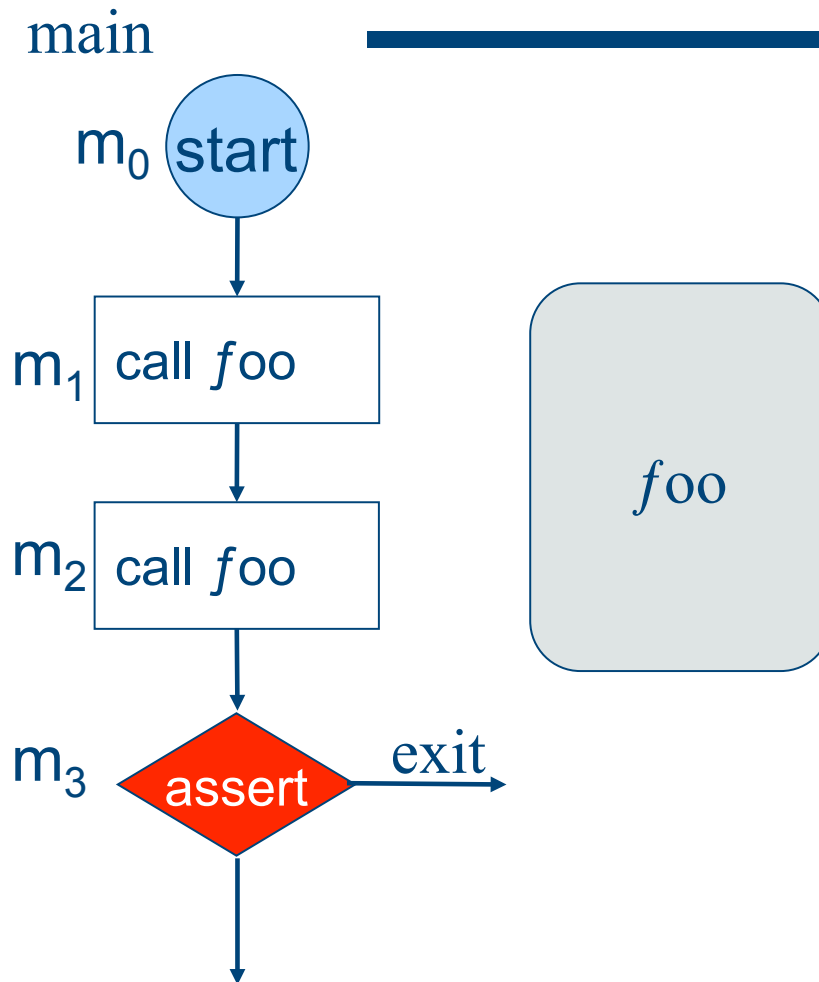


# Related Work on Heuristic estimates

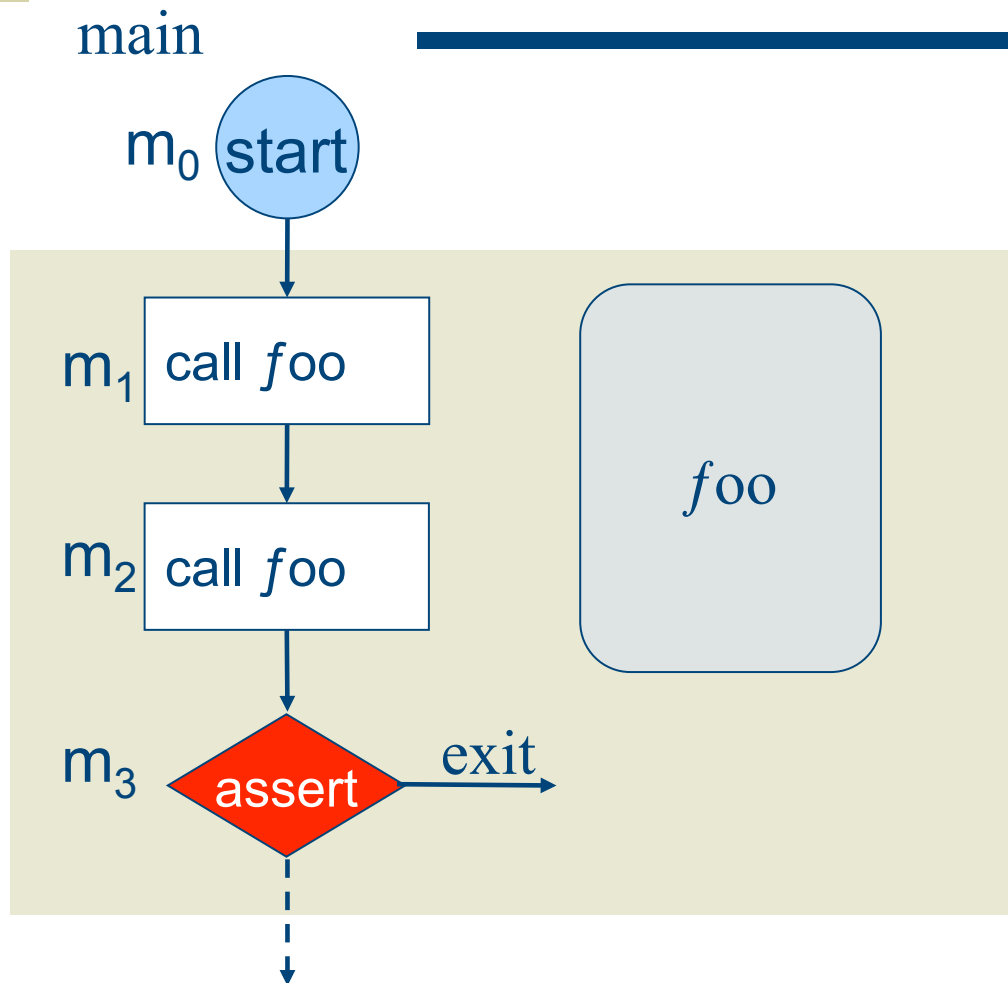
- ◆ *Edelkamp, Lafuente, and Leue*
- ◆ Minimum number of changes in program values
  
- ◆ *Seppi, Jones, and Lamborn*
- ◆ Use Bayesian reasoning
  
- ◆ *Visser and Groce*
- ◆ Structural properties of thread interdependencies
  
- ◆ *Edelkamp and Mehler*
- ◆ Minimal number of transitions (FSM distance)
  
- ◆ *Rungta and Mercer*
- ◆ Use partial context information to improve FSM distance



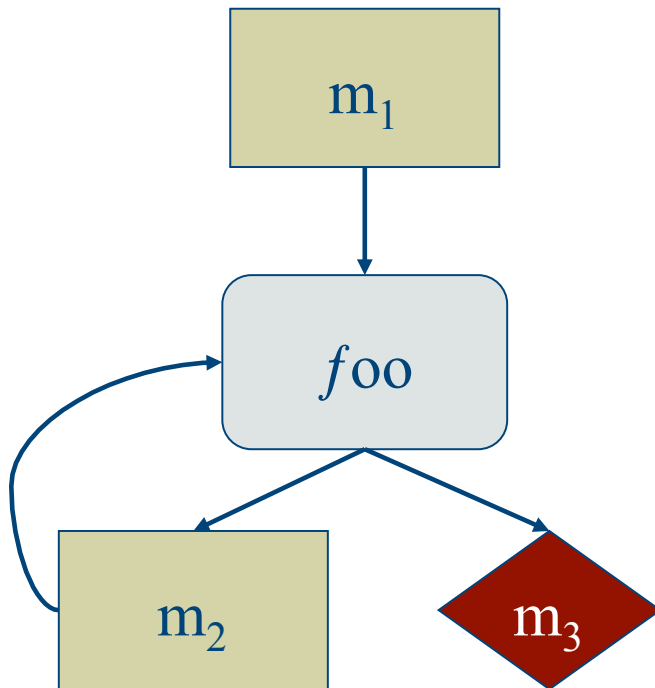
# FSM Distance Heuristic



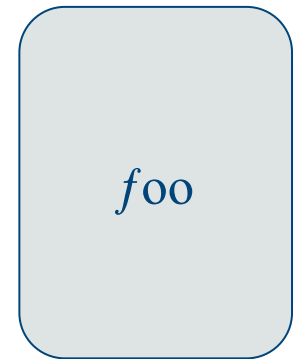
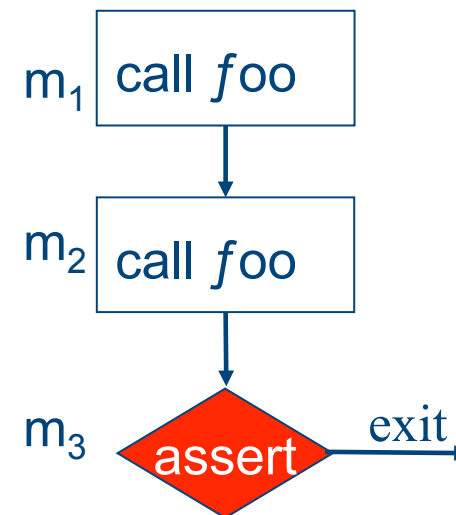
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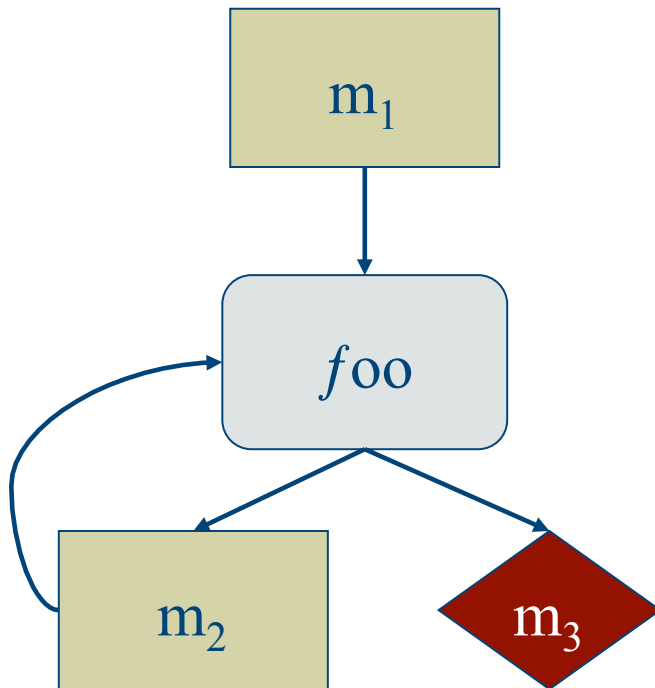


main



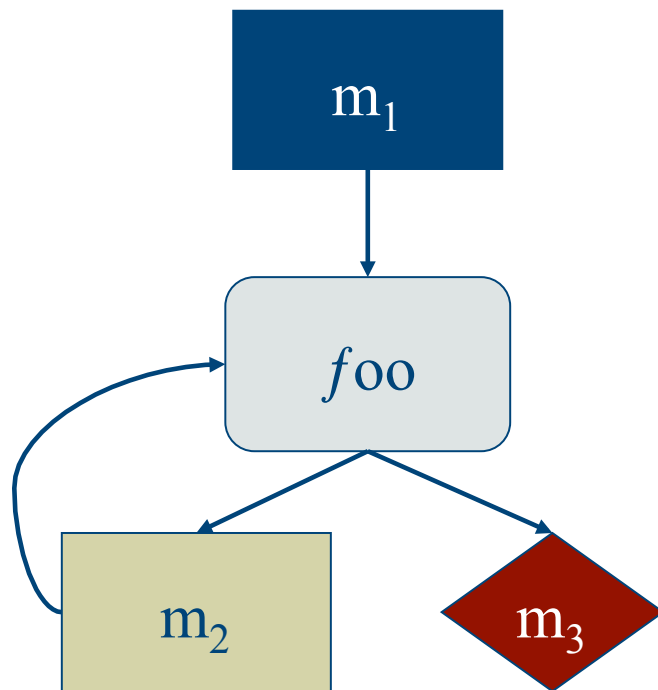


# FSM Distance Heuristic



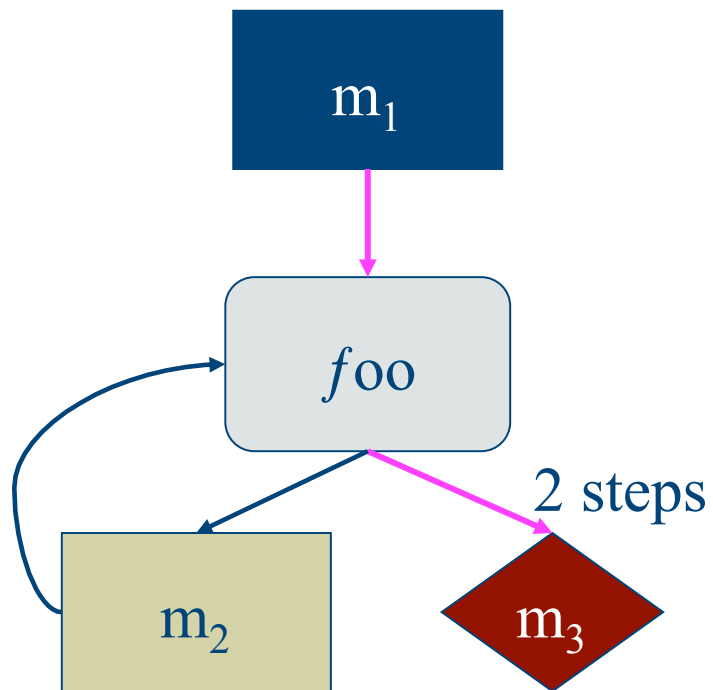
pc =  $m_1$   
x=1, y=2  
Runtime  
stack

# FSM Distance Heuristic



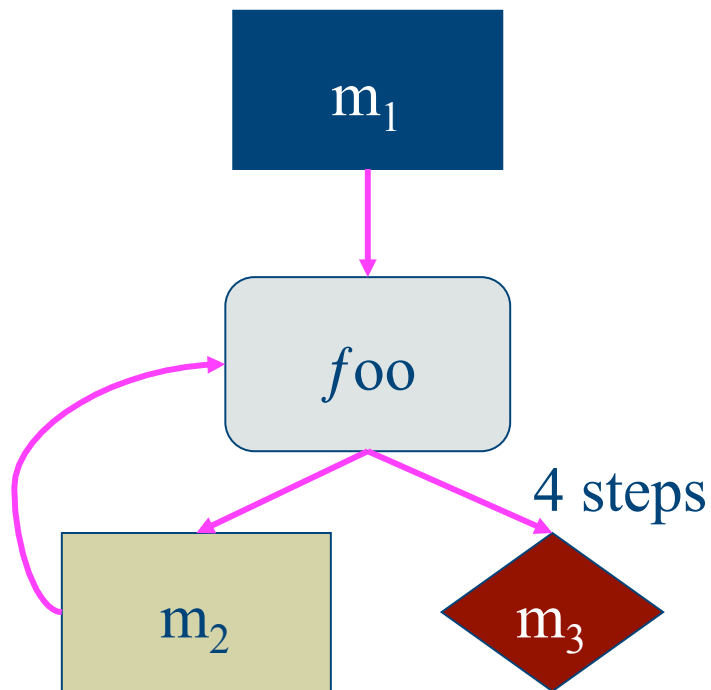
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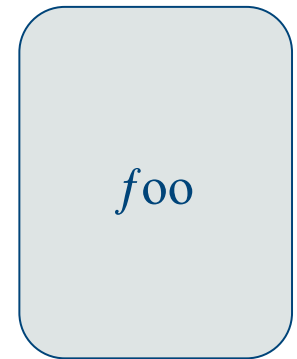
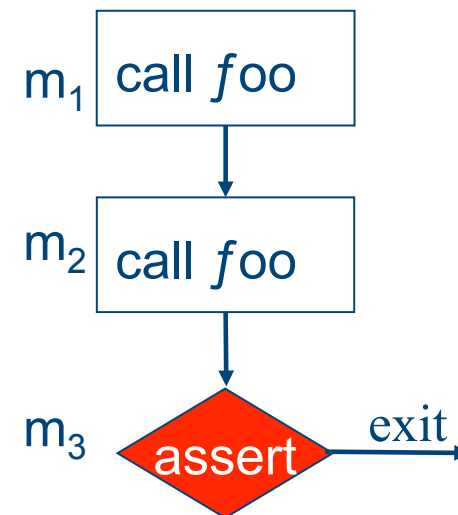


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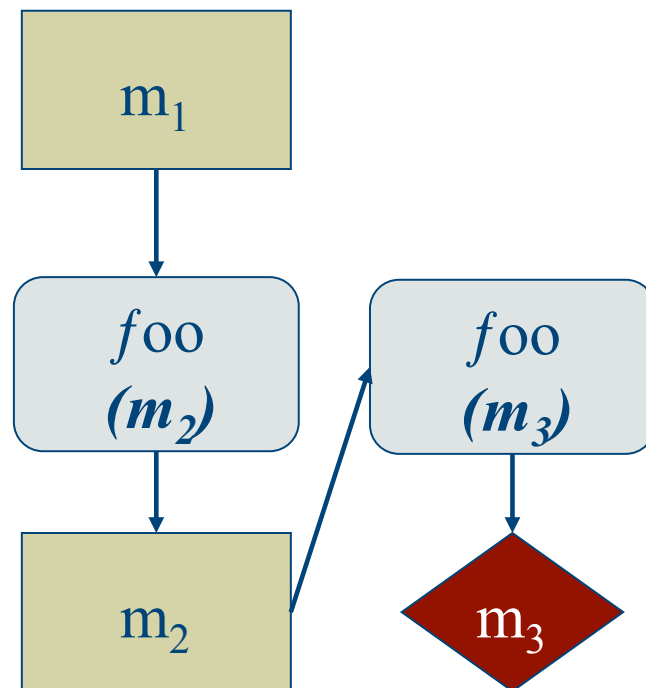
# Lack of Context



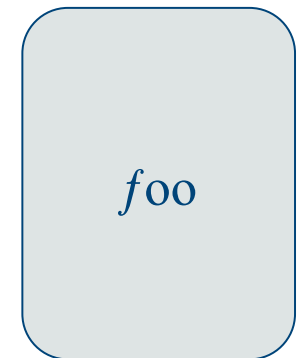
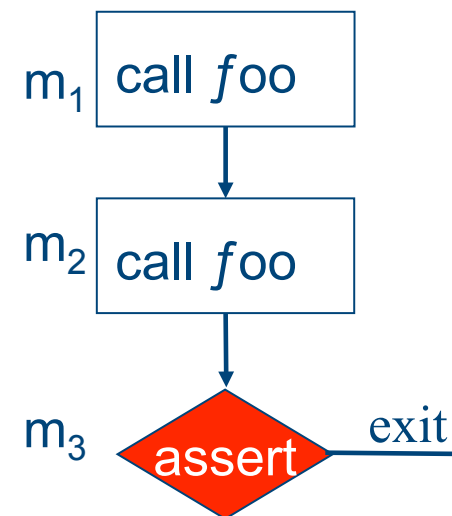
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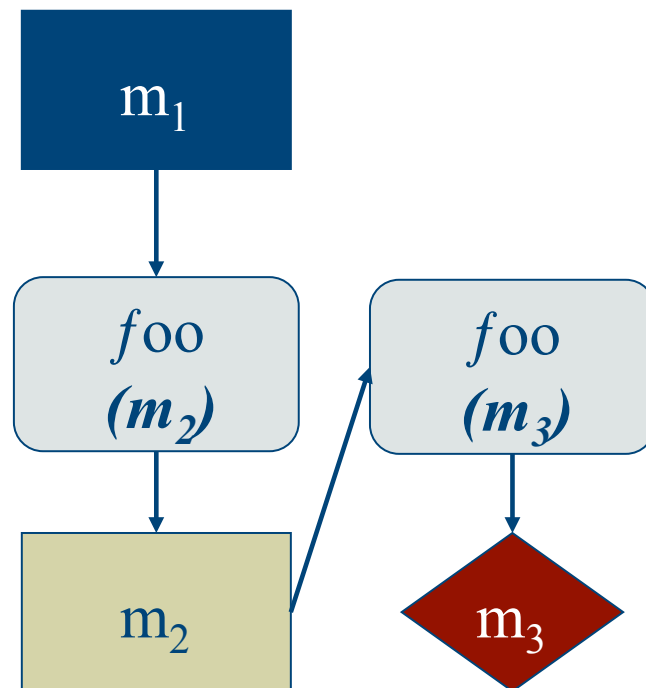
# $k$ -bounded Graph



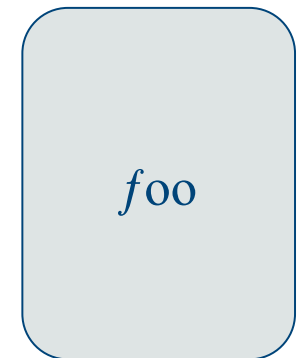
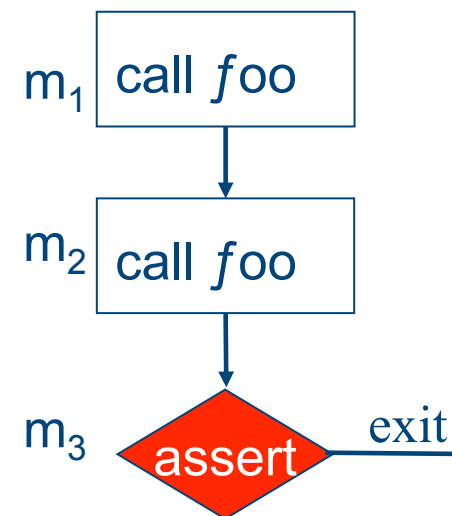
main



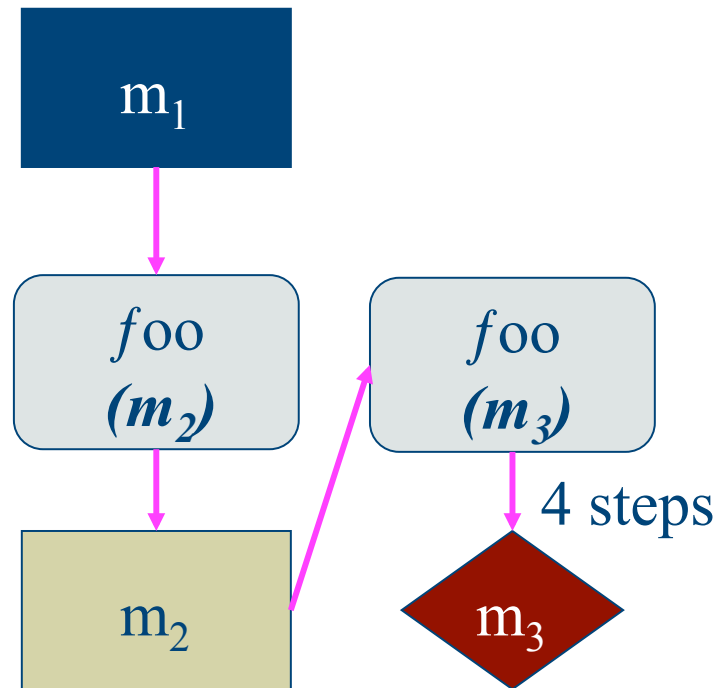
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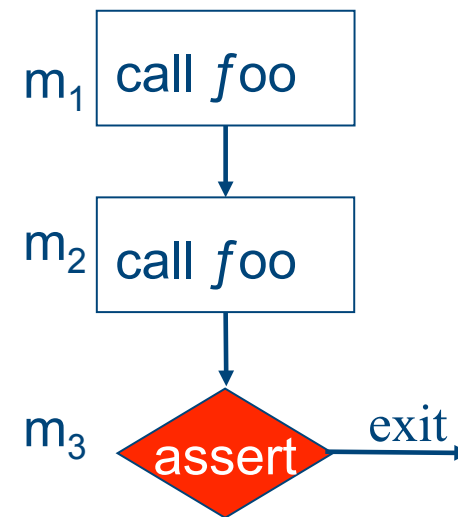
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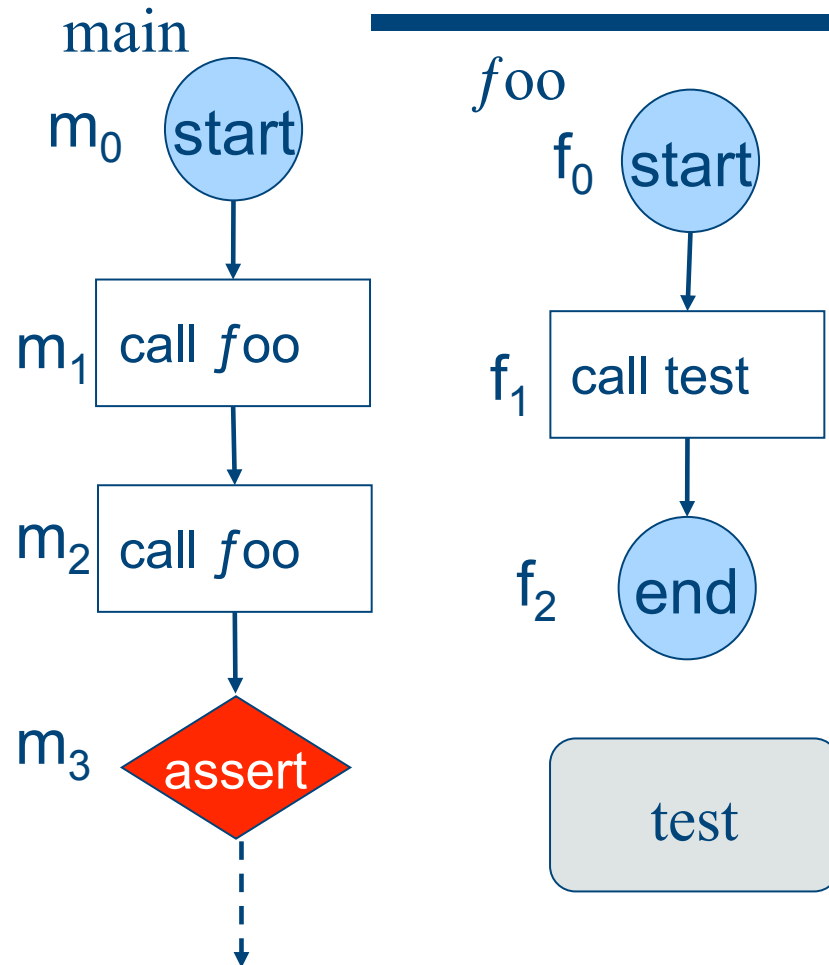
# *k*-bounded Graph



main

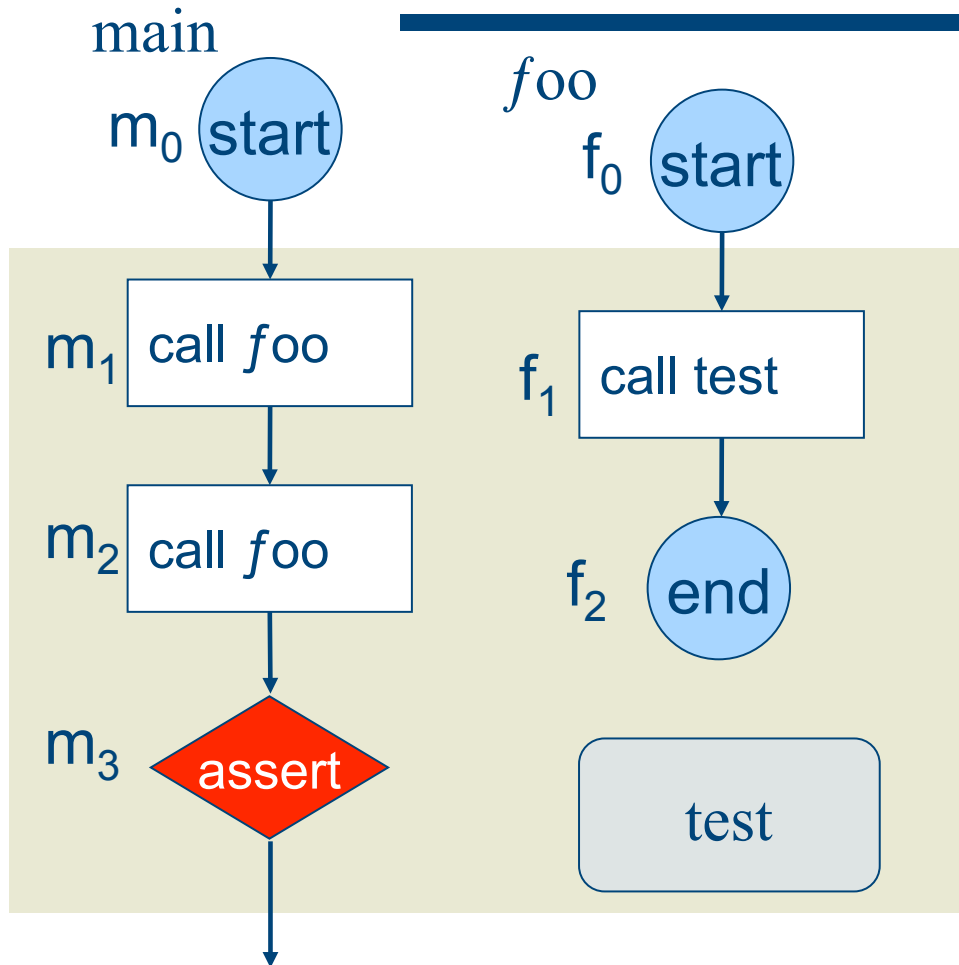


# EFSM Distance Heuristic

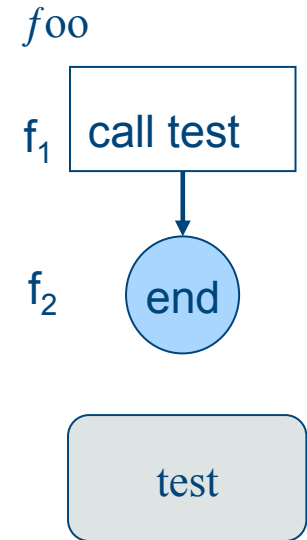
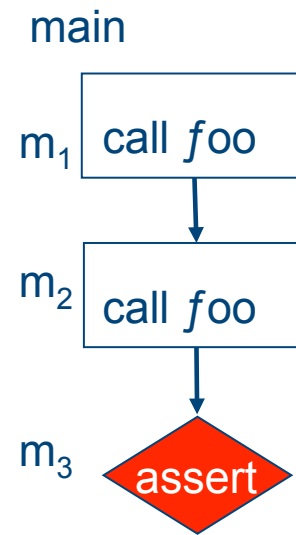
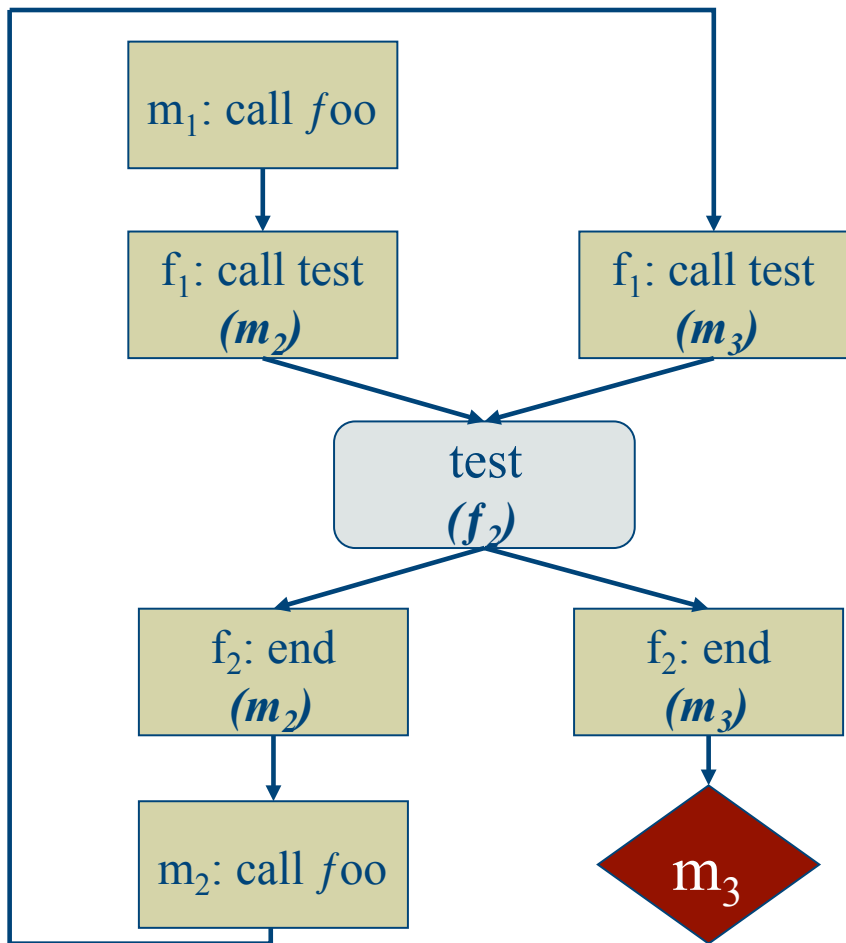




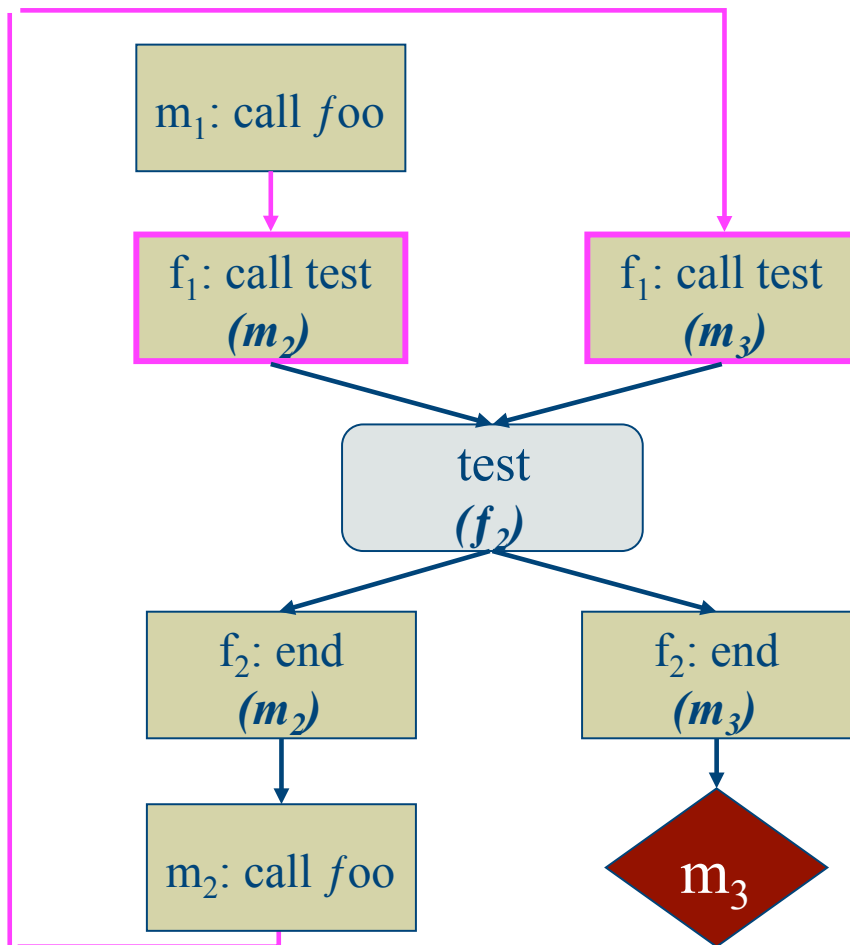
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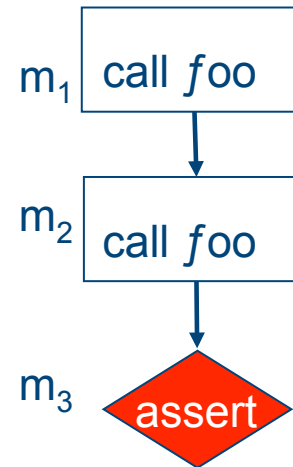
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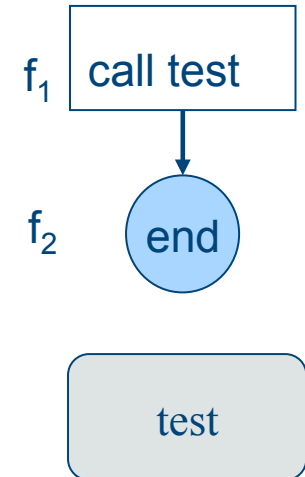
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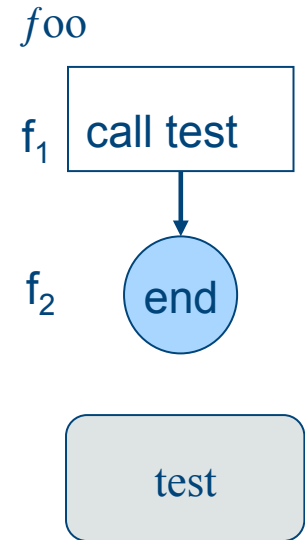
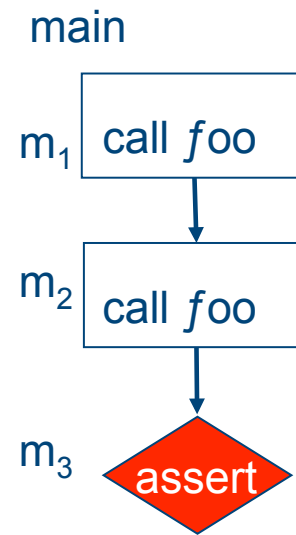
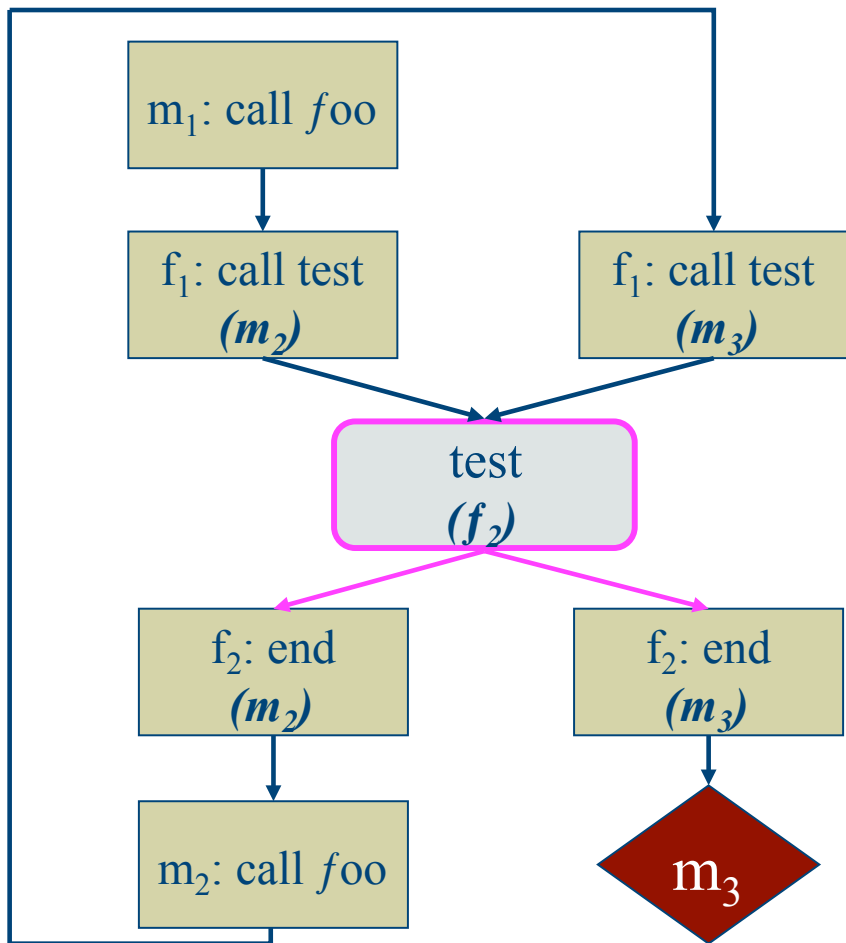
main



foo

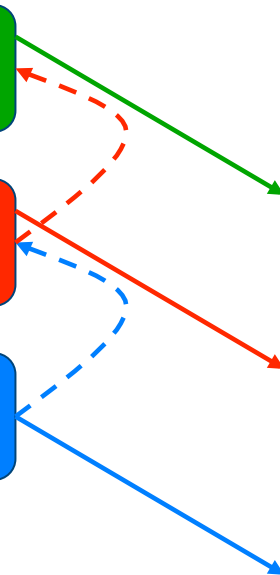
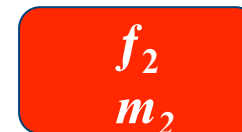
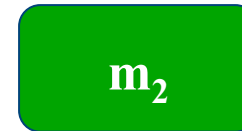
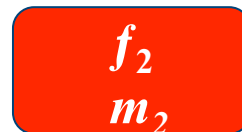
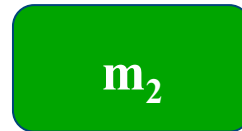


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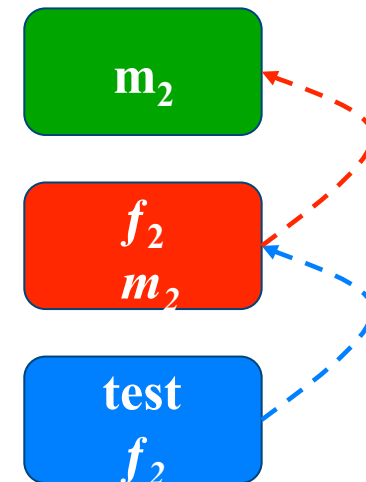
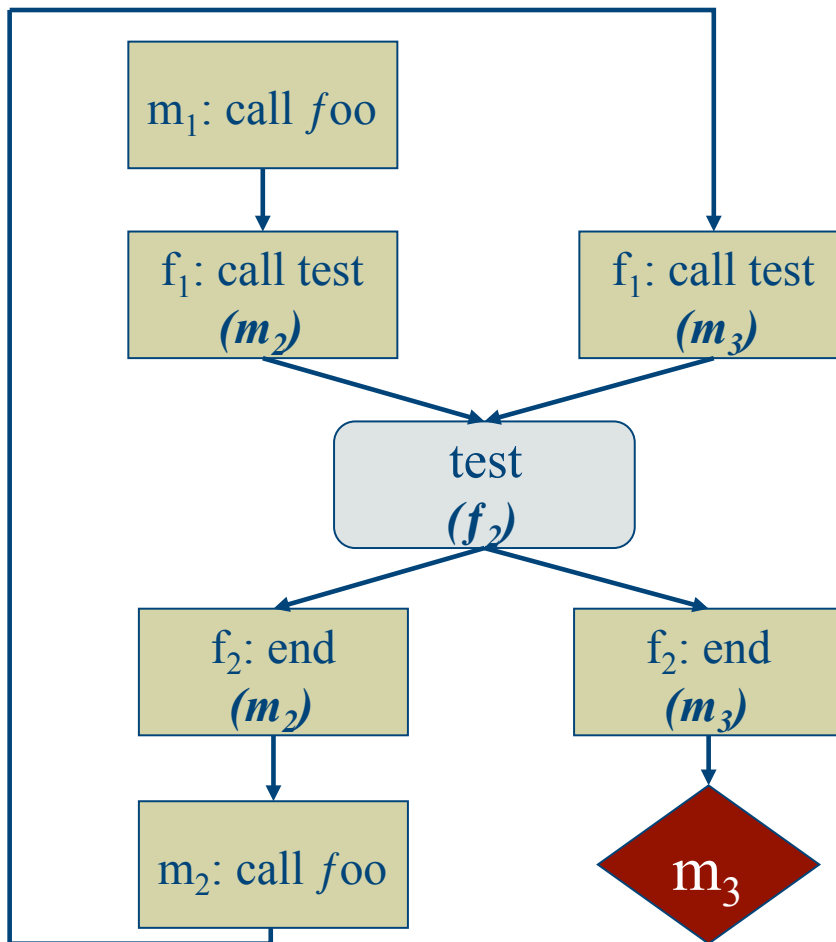


# Recreate the call trace

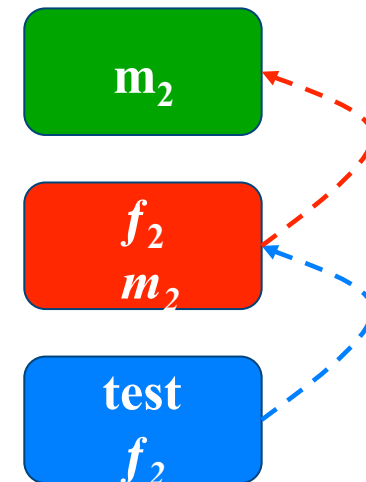
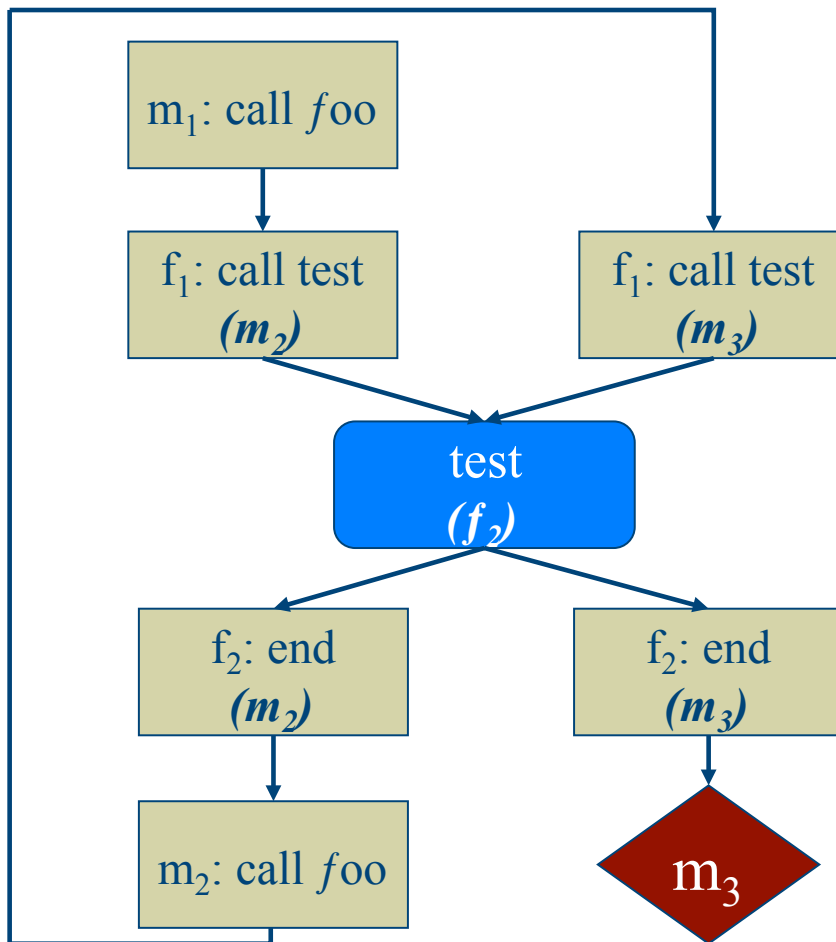
Stack frame for main
Return Add : $m_2$
Stack frame for <i>foo</i>
Return Add : $f_2$
Stack frame for test



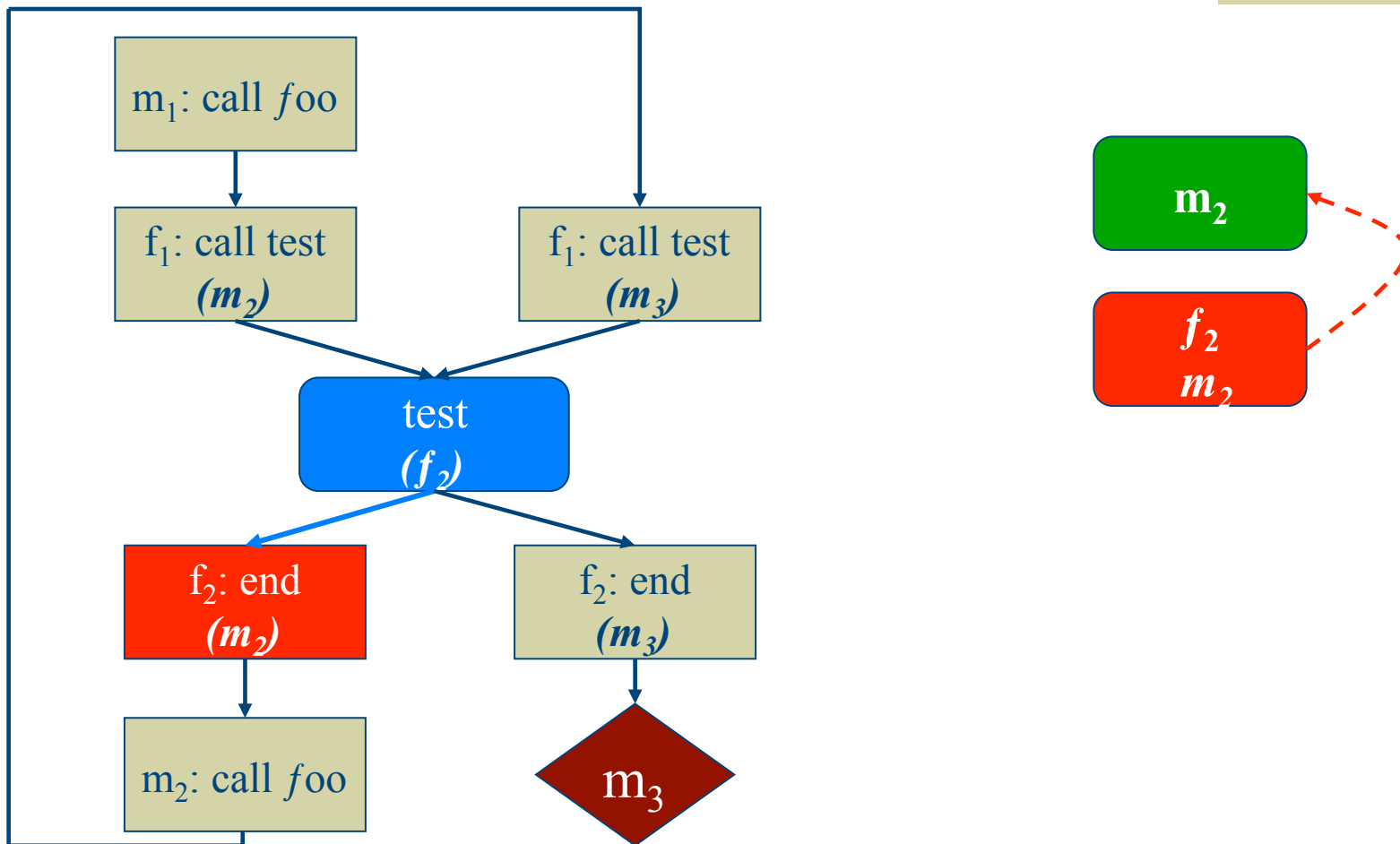
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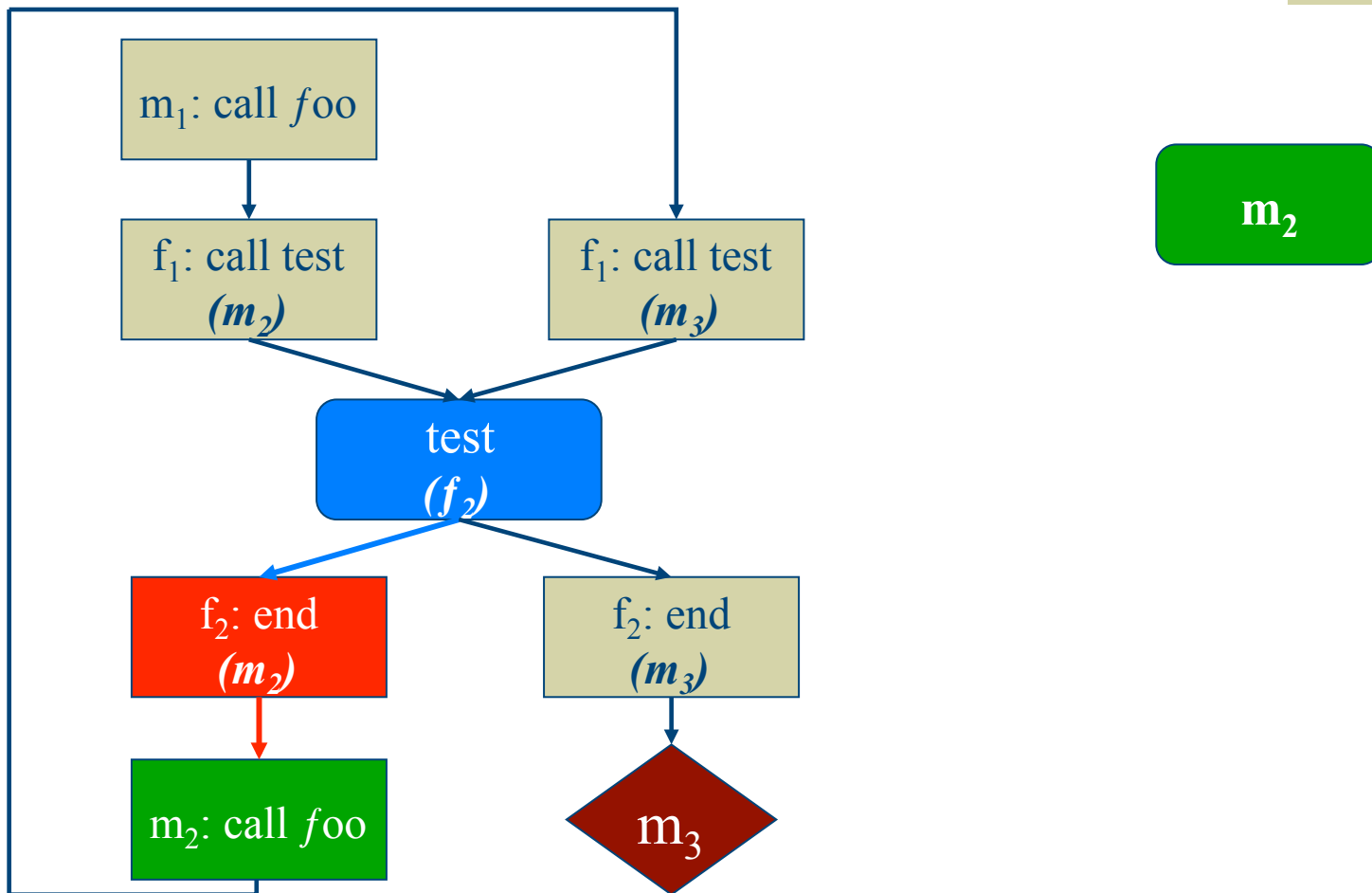


# EFSM Distance Heuristic

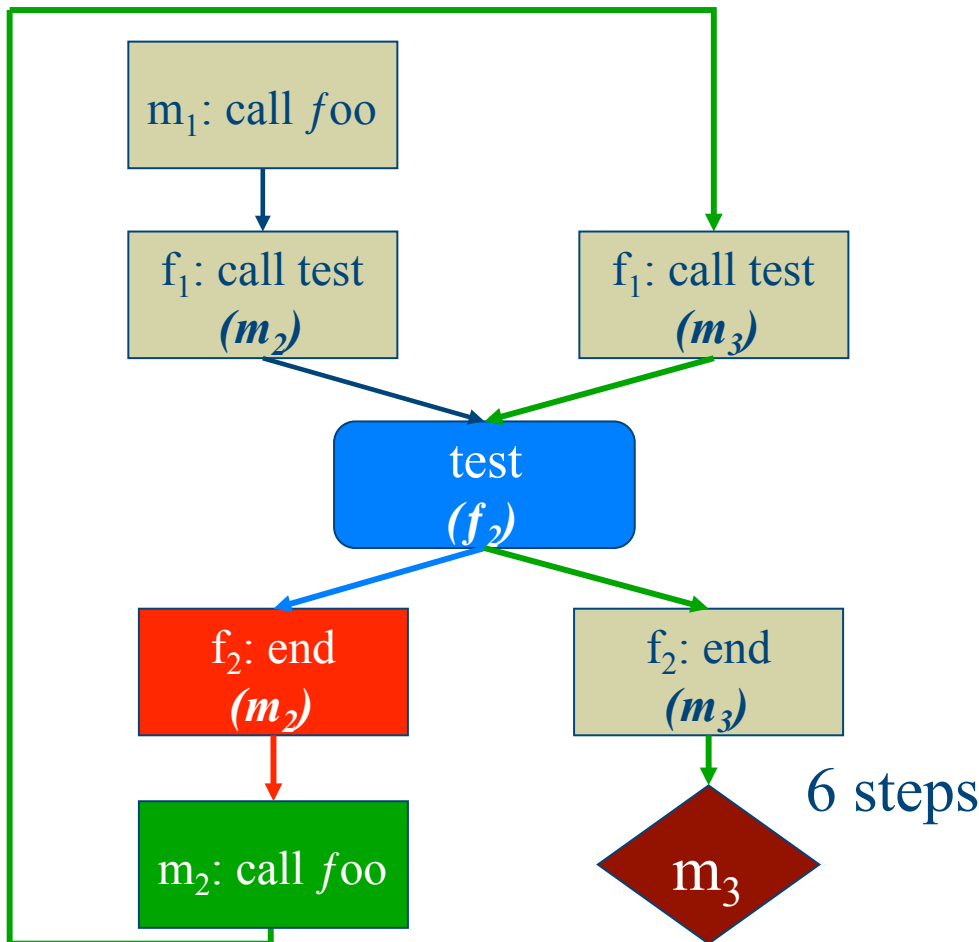




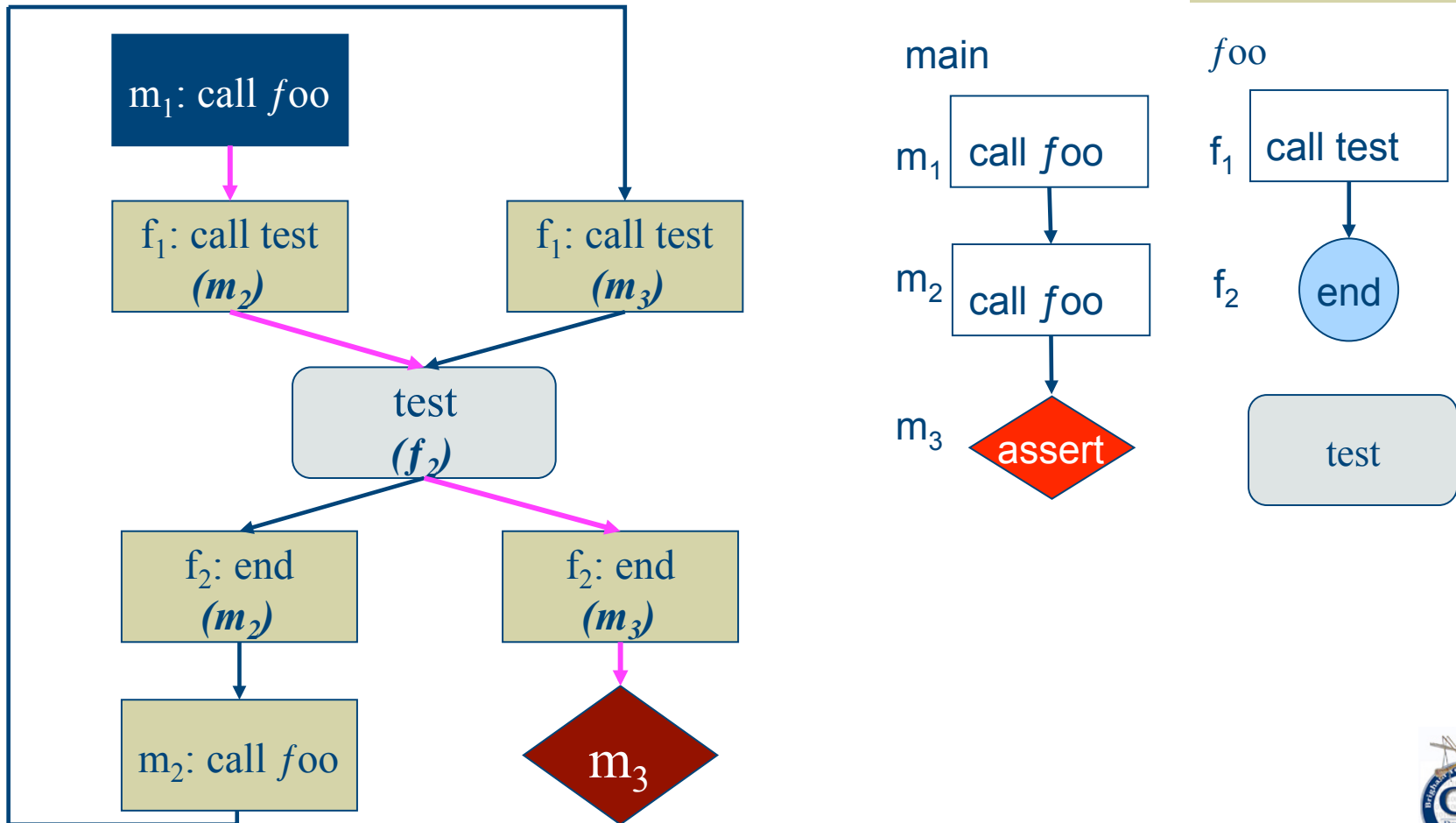
# EFSM Distance Heuristic



# EFSM Distance Heuristic the Heuristic



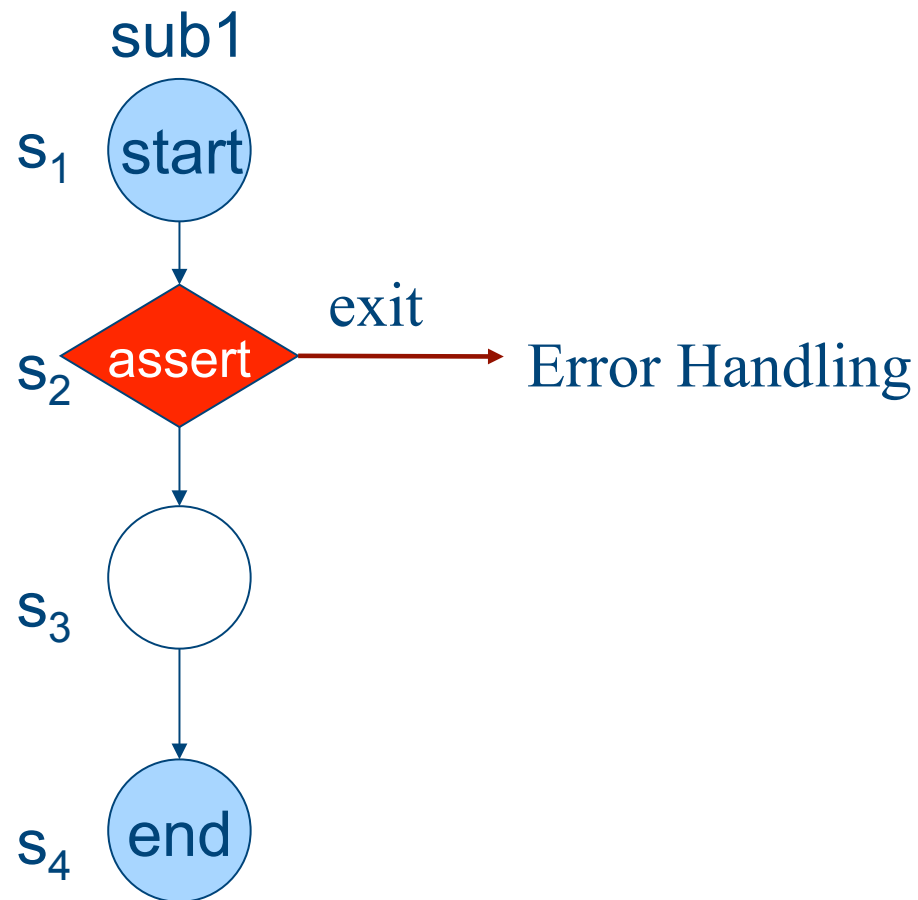
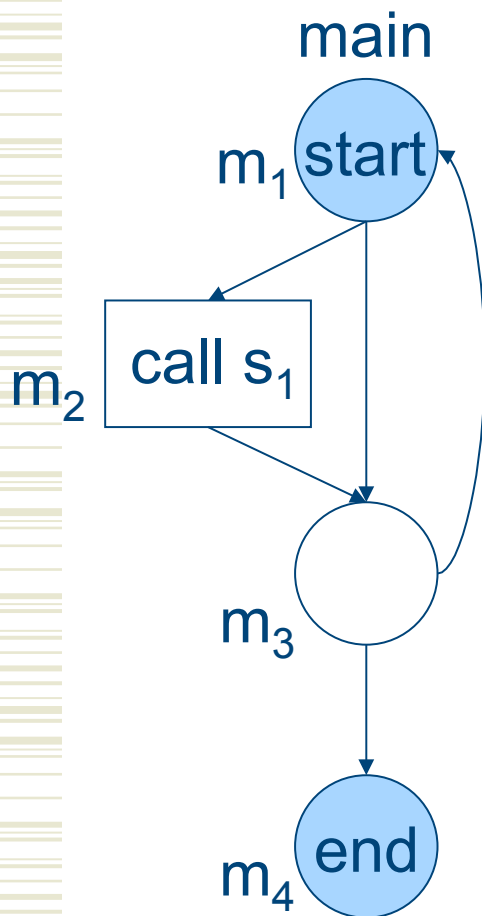
# Forward estimates are inaccurate



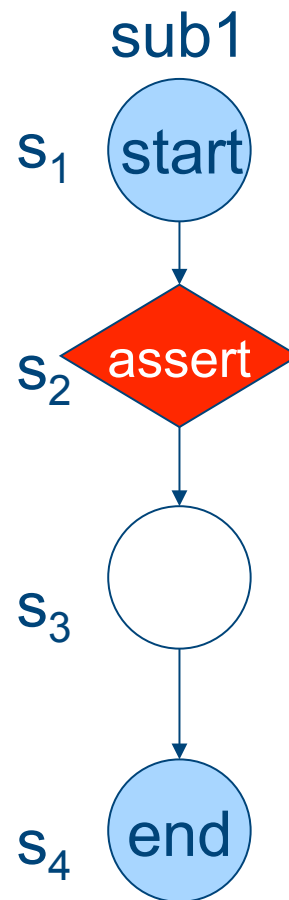
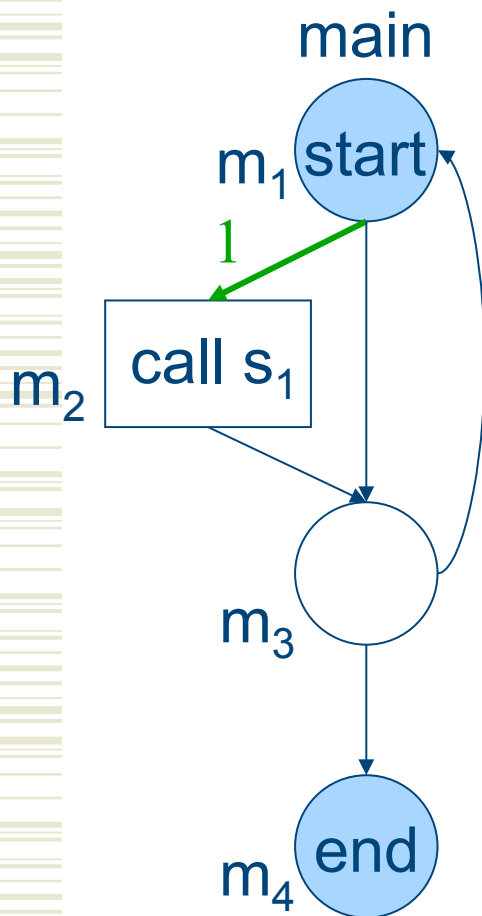
# Full Context Aware (FCA)

- ◆ Assume no recursion and resolved call-sites
- ◆ Statically compute distance estimates
- ◆ Full context information in the forward direction

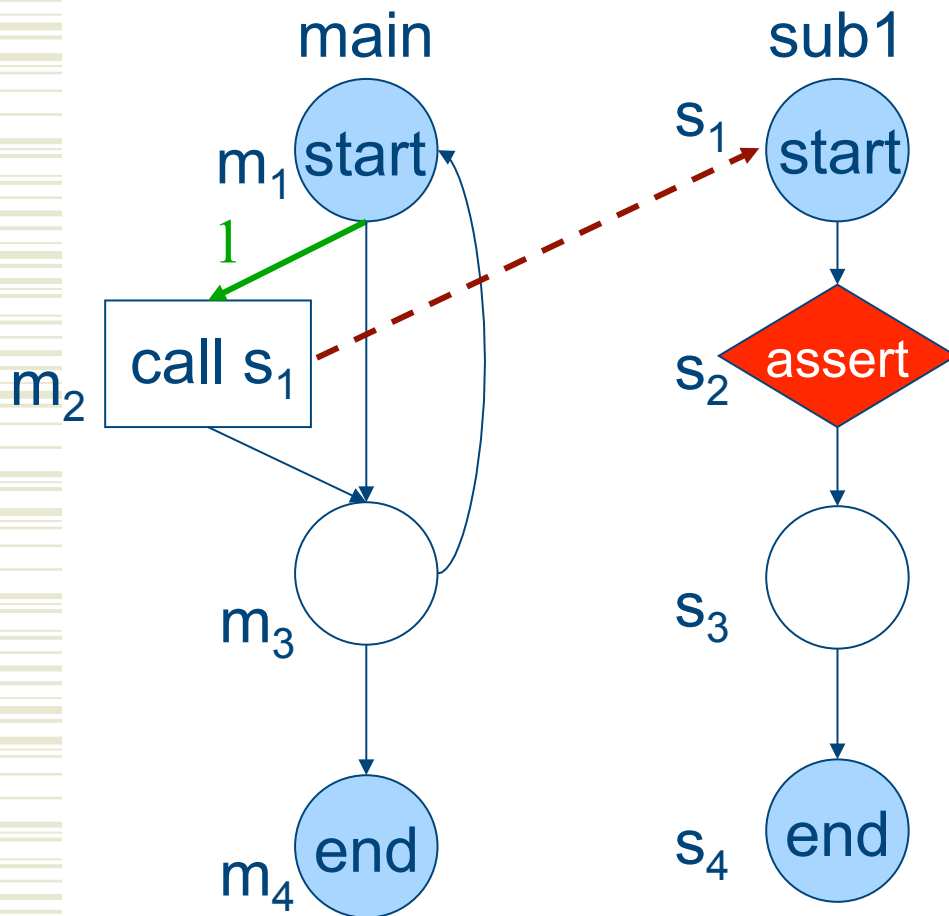
# Full Context Example



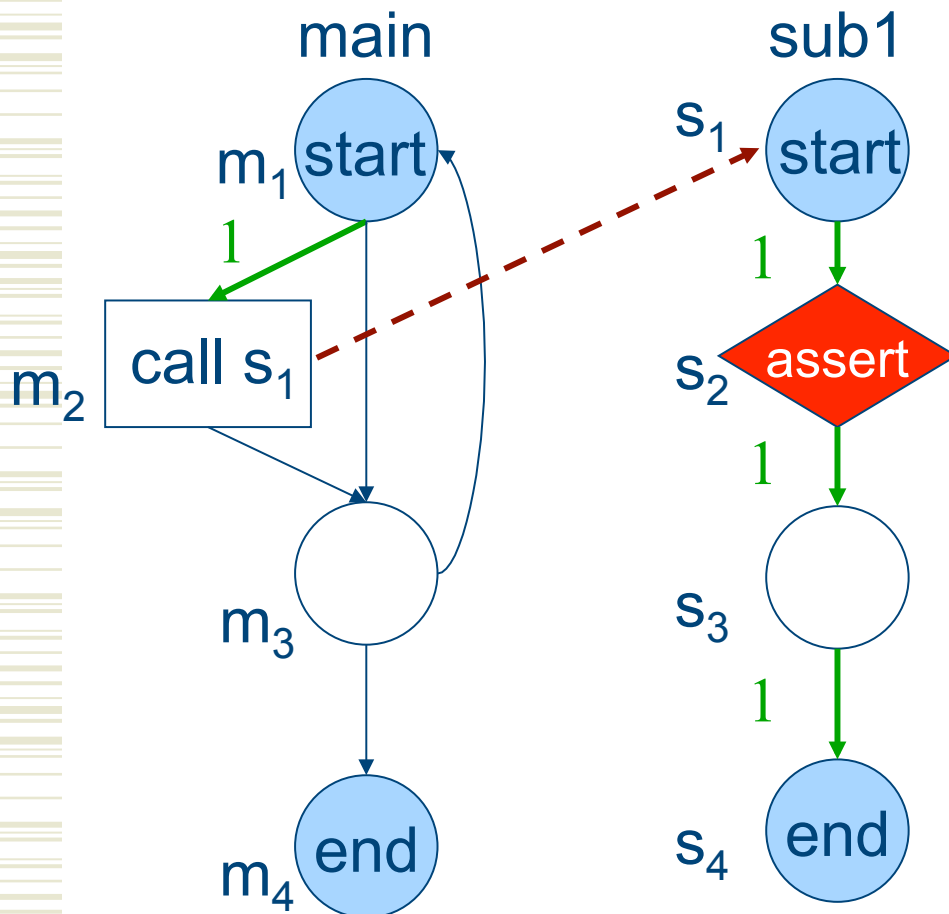
# Start DFS at Main CFG



# At Call node move to Target

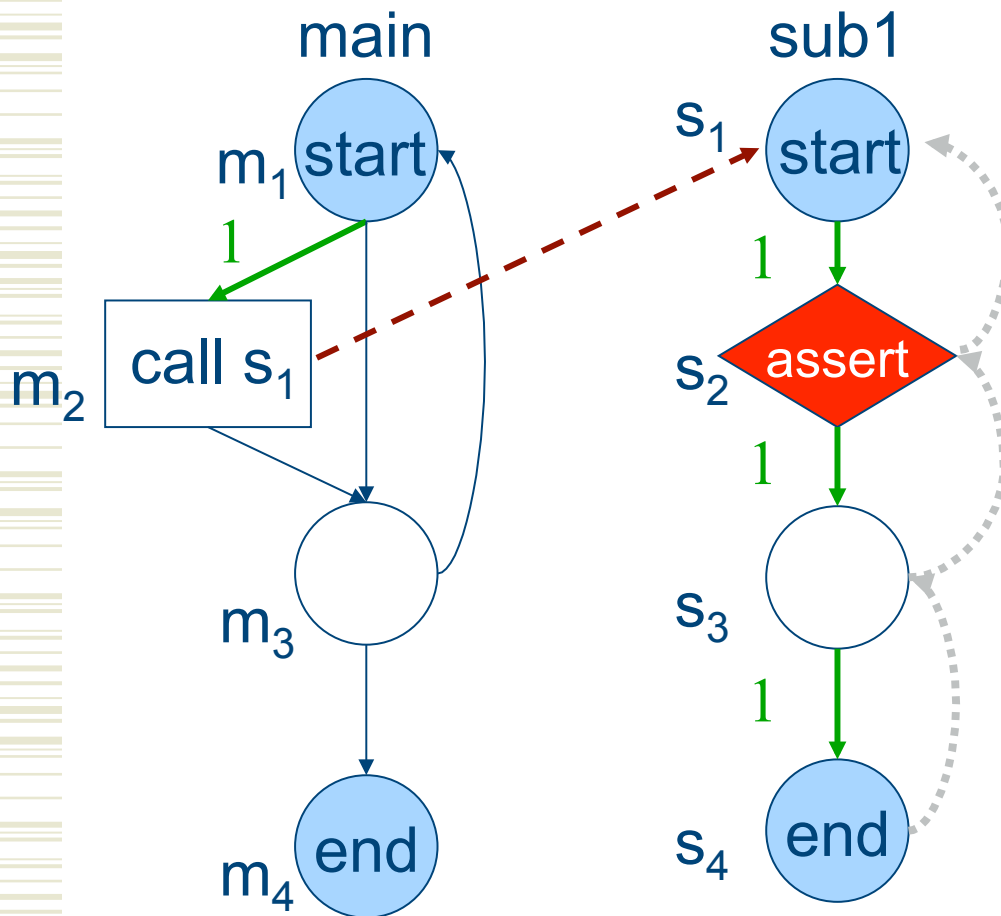


# Note the edge costs of nodes

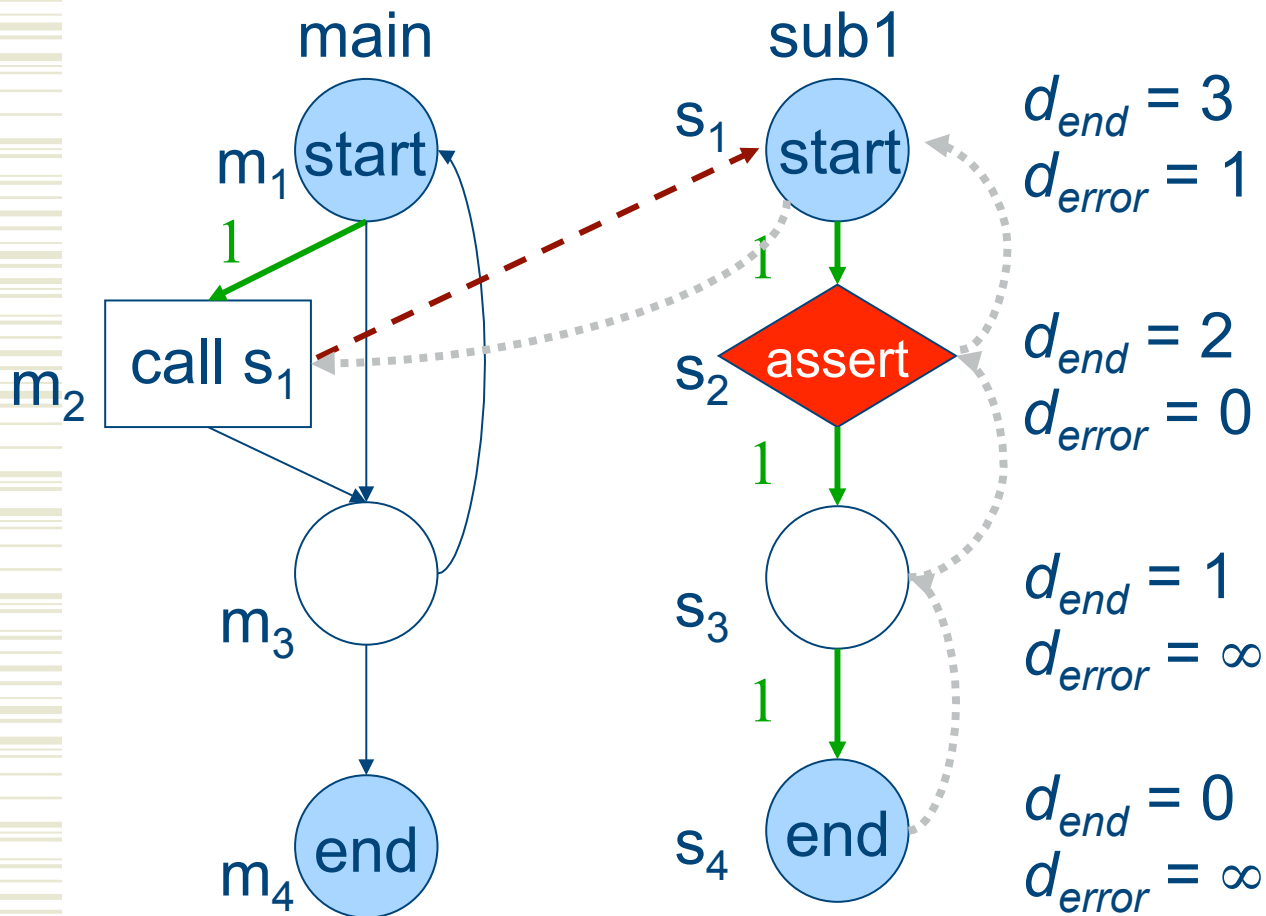




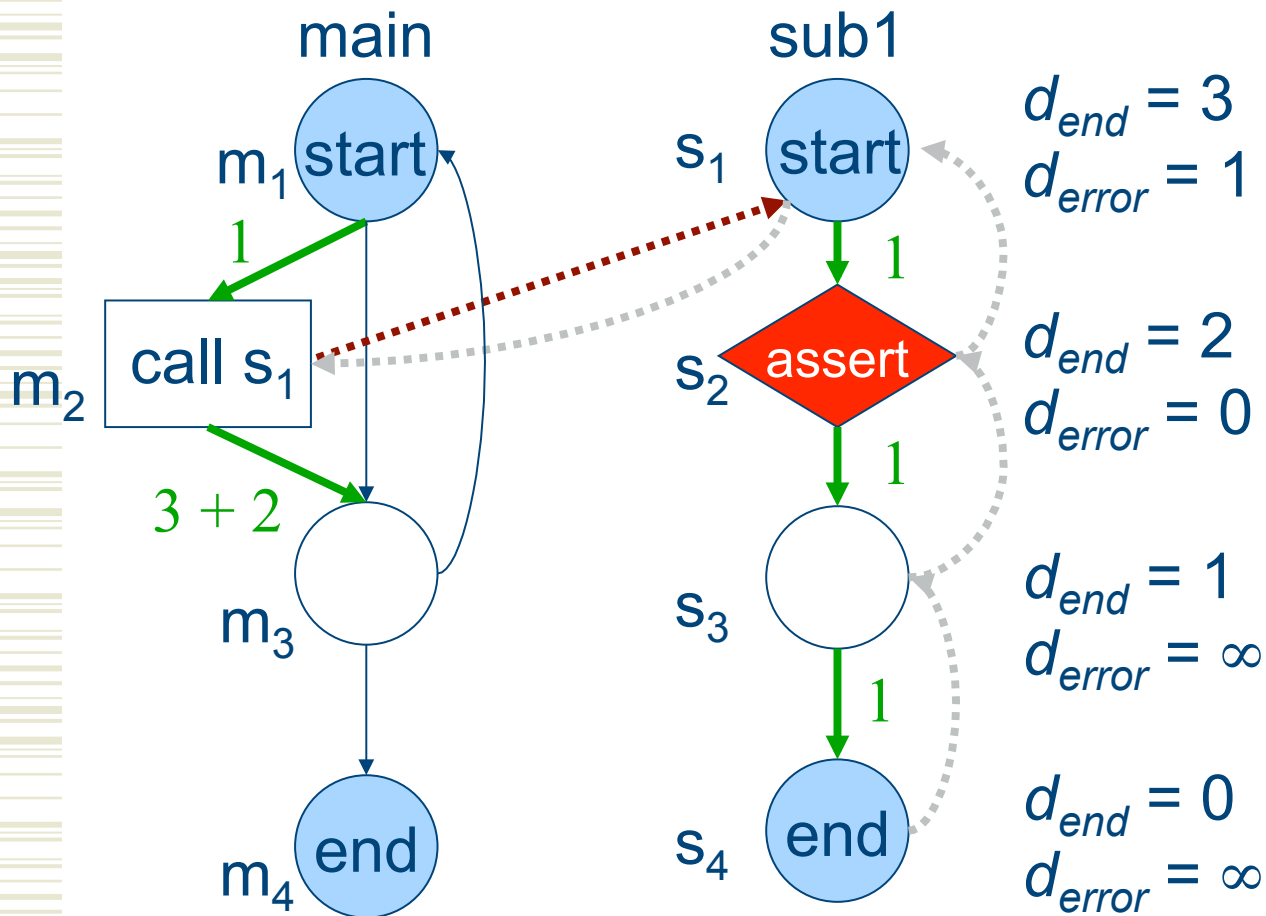
# Backtrack at end nodes



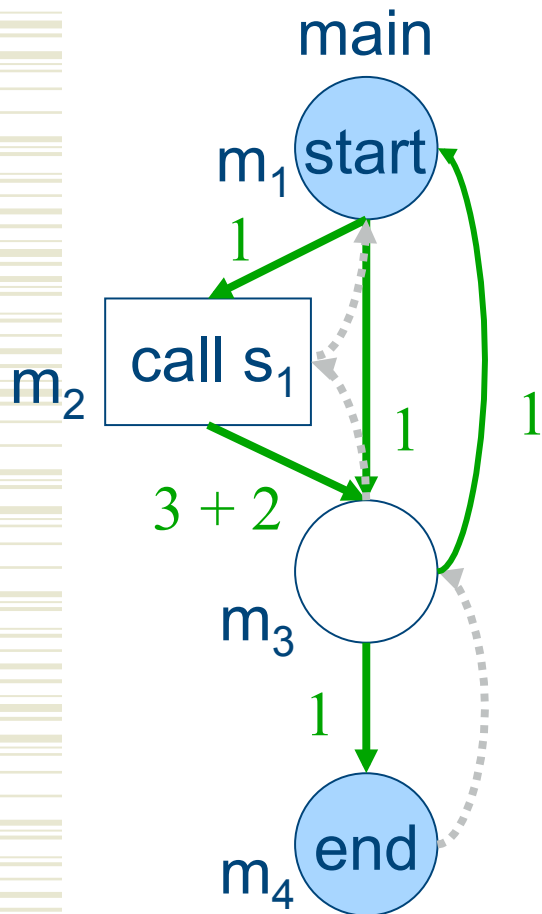
# All-pairs Analysis out of Start



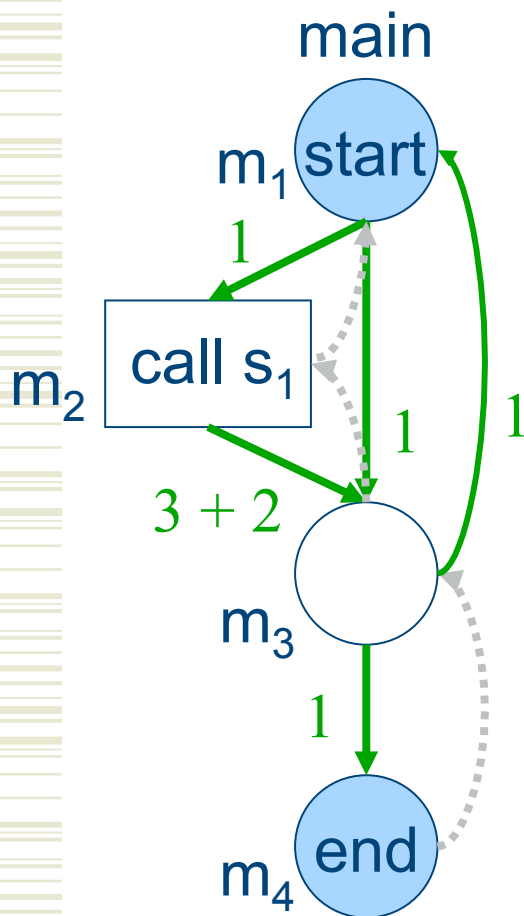
# Move Cost of Call to Call-site



# Continue Traversal



# Trigger All-pairs on Main CFG



$$d_{end} = 2$$

$$d_{error} = 3$$

$$d_{end} = 6$$

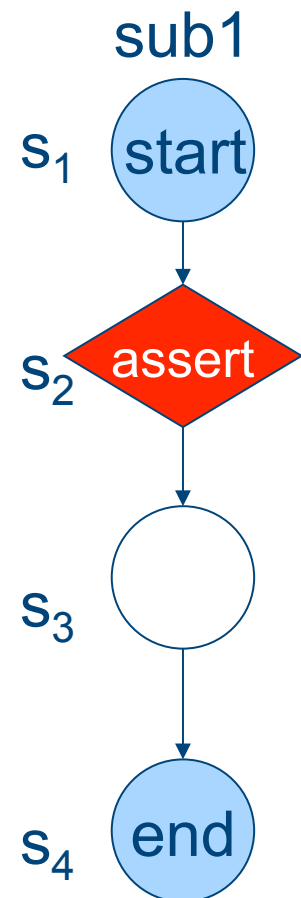
$$d_{error} = 2$$

$$d_{end} = 1$$

$$d_{error} = 4$$

$$d_{end} = 0$$

$$d_{error} = \infty$$



$$d_{end} = 3$$

$$d_{error} = 1$$

$$d_{end} = 2$$

$$d_{error} = 0$$

$$d_{end} = 1$$

$$d_{error} = \infty$$

$$d_{end} = 0$$

$$d_{error} = \infty$$

# Complexity

- ◆ Depth-first traversal:  $O(N+E)$
- ◆  $N$  and  $E$  for all nodes and edges
- ◆ All-pairs on local CFGs:  $O(N_i^3)$
- ◆ No exponential growth like the  $k$ -bound approach
- ◆ Scales better than  $k$ -bound approach
- ◆ Not limited to  $k$  anymore

# Performance Analysis

- ◆ M. Dwyer, S. Person, and S. Elbaum (FSE '06)
- ◆ Understand “hardness” of benchmark
- ◆ Measure error density with depth-bounded randomized DFS
- ◆ At each DFS level, pick random successor
- ◆ Run 1000 experiments on a cluster of machines
- ◆ Count number of experiments that find error
- ◆ Error density is ratio of error discovery runs to total experiments
- ◆ Hardness is inversely proportional to error density



# Super Computer

- ◆ Marylou 4 (among the top 50 supercomputers)
- ◆ 630 nodes with 2 dual core processors at 2.6GHz
- ◆ Each node has 8 GB RAM
- ◆ One hour time bound
- ◆ We get 1024 processors at a time.
- ◆ Makes testing go quickly for random experiments





# Random DFS vs. e-FCA

Depth = 2 Barbershop	e-FCA	Rand DFS Min over 1000 Runs	Rand DFS Average over 1000 Runs	Error Density over 1000 runs
T = 5	814	1,570	255,720	99.2%
T = 9	1,070	2,258	47,017	92.0%
T = 15	1,448	2,988	37,195	80.3%
T = 20	1,767	3,844	69,445	22.5%
T = 30	2,401	4,412	5,161	2.00%
T = 40	3,736	3,894	5,135	0.30%



# Guided Search Results

- ◆ FCA estimates used with runtime trace is e-FCA
- ◆ Use the gnu-debugger based model checker Estes
- ◆ Benchmark set of programs with concurrency errors
- ◆ Pentium III, 1.5 GHz processor with 2 GB of RAM
- ◆ NOTE: Still depend on default search order because we do not randomize ties in priority queue



# Time in seconds: Static analysis

Model	FSM	EFSM	e-FCA
Hyman (2) K=1 max=3	0	3	0
Hyman (2) K= 1 max=4	1	11	0
Hyman (2) K=1 max=5	1	27	0
Dining Phil (3) K=1 max=2	1	76	0
Dining Phil (3) K=1 max=3	1	146	0
Dining Phil (3) K=0 max=4	1	4	1
Dining Phil (3) K=0 max=5	2	7	1



# Time in seconds: Static analysis

Model	FSM	EFSM	e-FCA
Hyman (2) K=1 max=3	0	3	0
Hyman (2) K= 1 max=4	1	11	0
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Dining Phil (3) K=0 max=5	2	7	1



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Hyman (2) K=1 max=5	1	27	0
Dining Phil (3) K=1 max=2	1	76	0
Dining Phil (3) K=1 max=3	1	146	0
Dining Phil (3) K=0 max=4	1	4	1
Dining Phil (3) K=0 max=5	2	7	1



# Time in seconds: Static analysis

Model	FSM	EFSM	e-FCA
Hyman (2) K=1 max=3	0	3	0
Hyman (2) K= 1 max=4	1	11	0
Hyman (2) K=1 max=5	1	27	0
Dining Phil (3) K=1 max=2	1	76	0
Dining Phil (3) K=1 max=3	1	146	0
Dining Phil (3) K=0 max=4	1	4	1
Dining Phil (3) K=0 max=5	2	7	1



# States Generated before Error Discovery

Model	FSM	EFSM	e-FCA
Hyman (2) K=1 max=3	10,227	7,160	3,817
Hyman (2) K= 1 max=4	41,791	21,909	13,529
Hyman (2) K=1 max=5	123,743	59,951	38,745
Dining Phil (3) K=1 max=2	53,897	4,594	1,626
Dining Phil (3) K=1 max=3	54,725	13,830	3,816
Dining Phil (3) K=0 max=4	186,419	36,467	13,696
Dining Phil (3) K=0 max=5	334,198	400,474	55,876



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# Time taken in seconds before Error Discovery

Model	FSM	EFSM	e-FCA
Hyman (2) K=1 max=3	4	6	1
Hyman (2) K= 1 max=4	17	21	5
Hyman (2) K=1 max=5	49	56	16
Dining Phil (3) K=1 max=2	31	79	1
Dining Phil (3) K=1 max=3	28	155	3
Dining Phil (3) K=0 max=4	113	27	8
Dining Phil (3) K=0 max=5	178	388	32



# Time taken in seconds before Error Discovery

Model	FSM	EFSM	e-FCA
Hyman (2) K=1 max=3	4	6	1
Hyman (2) K= 1 max=4	17	21	5
Hyman (2) K=1 max=5	49	56	16
Dining Phil (3) K=1 max=2	31	79	1
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# Barbershop: scalability across threads

Thread No	Depth =2	Depth =5	Depth=9
5	814	7,064	92,434
15	1,448	7,698	93,608
20	1,767	8,071	93,927
25	2,086	8,336	94,246
30	2,401	8,970	94,561
40	3,040	9,603	92,500

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# Conclusions and Future Work

- ◆ e-FCA more efficient in our benchmarks
- ◆ Has some hope to scale to larger systems
- ◆ Works in the presence of PO reduction
  
- ◆ What else in the concrete state of use?
- ◆ What if we increase error locations?



# Questions

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