1 Project Description

The purpose of this project assignment is to (i) implement and apply the \textit{Multinomial Na"ive Bayes} (\textit{MNB}) model for text document classification and (ii) perform \textit{feature selection} on the vocabulary of a given document collection to reduce the training and test time of the MNB classifier without significantly affecting its accuracy.

You can implement this project in any programming language of your choice; however, you must follow the implementation specifications given in Section 2.

2 Implementing the Multinomial Na"ive Bayes Classifier

In this project, you are required to implement the MNB classifier, using the classes and methods specified in this section.

2.1 The MNB-classification class

This class is used for (i) training an MNB and (ii) classifying unlabeled documents using the trained MNB.

Given a document collection $DC$, which is a set of plain-text documents, all the stopwords in $DC$ are first removed. (The list of stopwords to be used is available at http://students.cs.byu.edu/~cs453ta/projs/stopwords.) Thereafter, $DC$ should be partitioned into two subsets: the $DC_{\text{training}}$ set, which contains 80\% of the documents randomly selected from $DC$, and the $DC_{\text{test}}$ set, which contains the remaining 20\% of the documents in $DC$. If you are using the entire vocabulary, i.e., when no \textit{feature selection} is applied, then a data structure $training\_set$ ($test\_set$, respectively), which includes the multinomial representation of each document in the $DC_{\text{training}}$ ($DC_{\text{test}}$, respectively) set should be created. (See a sample multinomial representation on Slide #14 in the Lecture Notes of Chapter 9). On the other hand, if \textit{feature selection} is applied, then the documents in the $DC_{\text{training}}$ set should first be used to determine the $selectedFeatures$ (as defined in the \textit{Feature Selection} method in Section 2.1.1). Hereafter, $training\_set$ ($test\_set$, respectively), which consists of the multinomial representation of each document in the $DC_{\text{training}}$ ($DC_{\text{test}}$, respectively) set using only the terms in $selectedFeatures$, should be created.

2.1.1 The featureSelection method

This method determines the words which should be chosen to represent documents in $training\_set$ and $test\_set$ based on the \textit{information gain (IG)} of each vocabulary\footnote{A \textit{vocabulary} consists of all the distinct words in the training portion of a document collection used for training an MNB model, i.e., the $DC_{\text{training}}$ set in this case.} term $w$, which is computed as follows:

\begin{equation}
IG(w) = - \sum_{c \in C} P(c) \log_2 P(c) + P(w) \sum_{c \in C} P(c|w) \log_2 P(c|w) + P(\bar{w}) \sum_{c \in C} P(c|\bar{w}) \log_2 P(c|\bar{w})
\end{equation}

where $C$ is the set of all classes in the document collection, $P(c)$ is the prior probability of class $c$, $P(w)$ is the prior probability of term $w$, $P(c|w)$ is the conditional probability of class $c$ given term $w$, and $P(c|\bar{w})$ is the conditional probability of class $c$ given term $\bar{w}$.
where \( C \) is the set of distinct natural classes in \( DC \), \( P(c) \) is the probability of the natural class \( c \), \( P(w) \) (\( P(\bar{w}) \), respectively) is the probability of occurrence (absence, respectively) of \( w \), and \( P(c|w) \) (\( P(c|\bar{w}) \), respectively) is the probability of \( c \) given that \( w \) is present (absent, respectively) in \( c \).

\[
P(c) = \frac{\text{# of documents in } DC_{\text{training}} \text{ labeled as } c}{\text{Total number of documents in } DC_{\text{training}}}
\]

\[
P(w) = \frac{\text{# of documents in } DC_{\text{training}} \text{ in which } w \text{ occurs}}{\text{Total number of documents in } DC_{\text{training}}}
\]

\[
P(\bar{w}) = \frac{\text{# of documents in } DC_{\text{training}} \text{ in which } w \text{ is absent}}{\text{Total number of documents in } DC_{\text{training}}}
\]

\[
P(c|w) = \frac{\text{# of documents in } DC_{\text{training}} \text{ in which } w \text{ occurs that are labeled as } c}{\text{Total number of documents in } DC_{\text{training}} \text{ in which } w \text{ occurs}}
\]

\[
P(c|\bar{w}) = \frac{\text{# of documents in } DC_{\text{training}} \text{ in which } w \text{ is absent that are labeled as } c}{\text{Total number of documents in } DC_{\text{training}} \text{ in which } w \text{ is absent}}
\]

The input of \textit{featureSelection} includes the \( DC_{\text{training}} \) set and a user-defined value \( M \) (\( \geq 1 \)) which denotes the number of words in the vocabulary that should be selected. (If \( M = |\text{Size of the Vocabulary}| \), then no feature selection is applied. Otherwise, \( M \) is one of the values specified in Section 3.) The output of \textit{featureSelection} is a data structure with \( M \) words, denoted \textit{selectedFeatures}, which are the words in the vocabulary with \( IG \) values higher than the other words in the \( DC_{\text{training}} \) set and are used to represent each document in \textit{training\_set} and \textit{test\_set}.

\subsection*{2.1.2 The label method}

This method assigns the most probable class for a particular document in \textit{test\_set}. In performing the classification task, you are required to use the \textit{getWordProbability} and \textit{getClass\_Probability} methods, which are defined in Sections 2.2.3 and 2.2.4, respectively.

The input of \textit{label} is a document \( D \) in \textit{test\_set}, and the output is the class \( c \) that should be assigned to \( D \).

\subsection*{2.2 The MNB-probability class}

This class is used for training an MNB.

\subsubsection*{2.2.1 The computeWordProbability method}

This method computes the probability of each distinct word in each natural class in \( C \) using \textit{training\_set}. In computing the word probabilities, you are required to use the Laplacian Smoothed Estimate. (See Slide #15 in the Lecture Notes.)

The input of \textit{computeWordProbability} is \textit{training\_set}, and the output is a data structure called “WordProbabilities,” which includes for each word in the vocabulary its probability for each class in \( C \).

\subsubsection*{2.2.2 The computeClassProbability method}

This method computes the probability of each natural class in \( C \) using \textit{training\_set}.

The input of \textit{computeClassProbability} is \textit{training\_set}, and the output is a data structure called “ClassProbabilities,” which includes the probability of each class in \( C \).
2.2.3 The getWordProbability method

This method retrieves the probability value of a word in a particular class, which includes the probability value of each word not seen during the training phase of MNB.

The input of getWordProbability includes a word w and a class c, and the output is the probability of w in c, which is stored in “WordProbabilities.”

2.2.4 The getClassProbability method

This method retrieves the probability value of a natural class.

The input of getClassProbability is a class c, and the output is the probability of c, which is stored in “ClassProbabilities.”

2.3 The MNB-evaluation class

This class computes the accuracy of the trained MNB in text document classification.

2.3.1 The accuracyMeasure method

This method computes the accuracy of the trained MNB. Accuracy is defined as the proportion of documents in test_set for which their classification labels determined using the trained MNB are the same as their pre-defined, i.e., original, labels over the total number of documents in test_set.

The input of accuracyMeasure is the set of documents in test_set and their labels determined by using the method label in MNB-classification, whereas the output is the classification accuracy of the documents in test_set.

3 Classification

Having implemented the MNB classifier following the specifications in Sections 2.1 and 2.2, you must

- Use the MNB model and the 5-fold cross validation approach to determine the classification accuracy and the training and test time based on a set of 10,000 documents in the 20NG dataset, which can be downloaded from http://students.cs.byu.edu/~cs453ta/projs/20NG.rar, without applying feature selection.

- Use the trained MNB and the 10,000 documents in 20NG to determine the effects of its accuracy, as well as its training and test time, when considering different vocabulary sizes. In accomplishing this task, use the 5-fold cross validation approach and for each one of the four vocabulary size values $M \in \{6200, 12400, 18600, 24800\}$ (i) perform feature selection, (ii) determine the classification accuracy, and (iii) determine the training and test time.

In the 5-fold cross validation approach, each experiment is repeated 5 times, i.e., each time a different subset of 20NG is used for the training and testing purpose. Thereafter, the averaged classification accuracy and the training and test time of each iteration should be reported.

4 Grading Criteria

The assignment is worth 150 points, and the breakdown of the point distribution is given below.

- Implementing the Multinomial Naïve Bayes Classifier is worth 120 points.
• Implementing Information Gain for feature selection is worth 30 points.

You are required to pass off your project with the TA during her office hours by the due date. Prior to passing off your Project 4 with the TA, you are required to prepare (i) a diagram which shows the accuracy of your MNB classifier with and without applying feature selection based on Information Gain, and (ii) another diagram which shows the training and test time using different vocabulary sizes, which should allow the TA to verify the correct implementation of your Project 4.

Hint: In verifying that your MNB implementation is working adequately, it is suggested that instead of using the subset of 10,000 documents in 20NG, you assess the classes and methods implemented for training and testing the MNB model using the documents shown in Slide #14 in the Lecture Notes of Chapter 9, which should significantly reduce the time spent in debugging the implementation of the MNB.