

**Artificial Intelligence**  
 CS 470  
 Instructor – Michael A. Goodrich

Name: \_\_\_\_\_

1. (10 points) (45 minutes) Do problem 17.1 in the book. Ignore the part about “projecting a hidden Markov model.”.
2. (10 points) (60 minutes) Do problem 17.4 in the book. For part b, rather than do the problem for an undiscounted MDP, assume  $\gamma = 0.9$ . Experience suggests that using a lot of paper will save you a lot of time.
3. (10 points) (45 minutes) Consider the following world.

13	14	15	16
9	10	11	12
5	6	7	8
1	2	3	4

In the figure, the numbers in each cell represent states. For example, the cell in the lower left hand corner is state  $s_1$ . The goal is in state  $s_{13}$  at the upper left. Consider the following policy:

$$\pi = \begin{cases} N & \text{for states 1-12} \\ W & \text{for states 13-16} \end{cases} .$$

The policy does not need to specify what to do in  $s_{13}$  since we assume that this state is an “absorbing state”, meaning that once this state is entered the agent will never leave. The reward structure for this problem is defined as follows:

$$r(s, a) = \begin{cases} 1 & \text{when state is } s_{14} \text{ and action is } W \\ 1 & \text{when state is } s_9 \text{ and action is } N \\ 0 & \text{otherwise} \end{cases} .$$

The world is deterministic except at state  $s_1$  and state  $s_6$ . At these states, the transition probability is as follows.

$P(s' s_1, N)$	$P(s_5 s_1, N) = 0.8$	$P(s_2 s_1, N) = 0.2$
$P(s' s_6, N)$	$P(s_{10} s_6, N) = 0.7$	$P(s_7 s_6, N) = 0.3$

Find the expected value,  $U(s, \pi)$ , of applying this policy from state  $s_1$  given a discount parameter of  $\gamma = 0.9$ .

4. (10 points) (10 minutes) Which actions are not dominated?

Utility/action	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$
$\mathcal{U}_1$	1	2	3	4	5
$\mathcal{U}_2$	-1	-2	-3	-4	-5
$\mathcal{U}_3$	0	6	0	4	2